

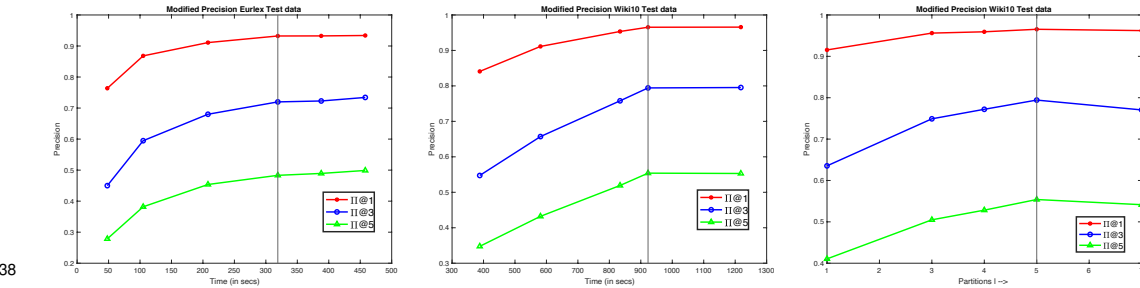
1 We thank the reviewers for their valuable time and thoughtful feedback. We are encouraged by the positive comments  
 2 w.r.t. our novel ideas and application of group testing to multilabel classification (MLC)([R3],[R4]), our method’s  
 3 scalability ([R4]), impressive runtimes ([R2]), and efficiency ([R3]). Please see our response below:

4 [R1],[R2],[R3] **Novel Contributions:** Our main contributions are: (a) the development of a (non-trivial) data-dependent  
 5 group testing scheme, that improves label grouping for MLGT significantly (vs. [35]), and can use the recently proposed  
 6 log-time decoding algorithm; (b) the use of matrix reordering techniques to hierarchically partition the label space, so  
 7 that we can apply MLGT to subsets of labels independently, in order to scale to very large label sets. These innovations  
 8 lead to a significantly faster training algorithm (Table 3) compared to most existing methods ( $\sim 50\text{min}$  vs.  $370\text{-}730$  hrs  
 9 for DISMEC, which has the highest accuracy), yet yield comparable results. Note that (more accurate) OvA methods  
 10 require  $O(d)$  classifiers to be trained (taking many hours). The tree methods use k-means clustering to create label  
 11 clusters (we use fast matrix reordering heuristics) and OvA classifiers at each leaf nodes (# classifiers  $\sim o(d)$ ) vs. our  
 12  $O(k \log d)$ ). Our method also has a provably log-time prediction algorithm, enabling almost real-time predictions.

13 [R1],[R2],[R3] **Similarity to [35]:** As we build on the MLGT algorithm of [35], where group testing was first proposed  
 14 for MLC, the core idea of creating  $O(k \log d)$  label groups is similar. However, the method in [35] yields poor accuracy  
 15 on large datasets due to random label grouping, and does not scale to extreme settings. We overcome these issues by first  
 16 developing a data-dependent grouping scheme (NMFGT) to improve the method’s accuracy, and then use hierarchical  
 17 partitioning to scale the method to very large problems. Sampling a group testing matrix that (a) captures the label  
 18 correlations, (b) has distinctive columns, and (c) satisfies the SAFFRON construction, is non-trivial. We propose a  
 19 technique that uses a normalized NMF basis (capturing label correlations) as a potential function for sampling columns  
 20 of the GT matrix that are distinct and have fixed average sparsity  $c$  (left regular graph). Computing a good GT matrix  
 21 via NMF for large  $d$  is difficult, and we use label partitioning in order to apply NMF-based MLGT to smaller problems.

22 [R1] **Weakness 1,2:** We develop the NMFGT and *also* the HE-NMFGT (NMFGT + hierarchical partitioning) to (a)  
 23 tackle large datasets and (b) get better accuracy on large datasets, and thus describe both. **Weakness 3 - Experimental**  
 24 **study:** We first show that NMFGT is better (See Fig 2. & suppl.) than earlier GT method in [35]. Also, SP-GT  
 25 results do not match with [35] as the modified prediction algorithm in this paper is better (we get better accuracy than  
 26 [35,Table 1]). We next use label partitioning to improve over NMF-GT for larger datasets (Table 2). Finally, we show  
 27 that partitioning+NMFGT has *significantly faster* training and prediction times than other methods (Table 3). We  
 28 believe that low training times (saving many hours) and fast predictions in return for a limited loss (few points) in  
 29 accuracy will be critical in many "related search" applications. **Weakness 4:** We use HE-NMFGT only when # labels is  
 30 too large to apply NMFGT. We do mention that for Mediamill and RCv1x there were no clear label partitions.

31 [R3], [R4] **Trade off and improvements:** We thank the reviewers for these suggestions. In the figures below we plot  
 32 precisions ( $\Pi@1, \Pi@3, \Pi@5$ ) versus runtimes (in secs) for Eurlex (left) and wiki10 (middle) datasets, by increasing  
 33 # groups  $m$  in each partition. Indeed, we notice a clear trade-off: as we increase runtimes, accuracy improves. But  
 34 beyond a point, the accuracy gain is limited as  $m$  is increased. In the paper, we chose smallest  $m$  (vertical line) for  
 35 which our accuracy is close to the SOA tree methods. Improved accuracy can be achieved for higher runtimes (when  
 36  $m$  is much more than  $k \log d$ ). We also plot  $\Pi@k$  versus # partitions  $\ell$  for Wiki10 (right). For smaller  $\ell$ , it is hard to  
 37 compute a good NMF for large matrices, and with many partitions, we will miss certain label correlations.



39 [R4] **Solution merger:** The output of MLGT will be a binary vector  $\{0, 1\}^{d_i}$ , hence, comparing scores across disjoint  
 40 subsets of labels will not an issue. For the shared labels across partitions, we indeed use weights for the label outputs  
 41 such that these weights add to 1. Due to space constraints these details were only briefly discussed (in sec. 4). **Label**  
 42 **partitions:** The matrix reordering method recursively partitions the labels, hence discovering a hierarchy. The code we  
 43 use produces the partitions (and sizes), in addition to the permutations depicted in Fig. 1. So the process is automatic.

44 [R2] **Ensemble methods, missing details/comparisons:** The ensemble idea is an exciting direction we have not  
 45 investigated! Linear SVM was used for classifiers (same as SOA tree methods). For large datasets the partition sizes  
 46 were  $\sim 40k$  labels. We had to defer the implementation details to supplement due to space constraints. We will include  
 47 a comparison to AnnexML (Tagami, 17) if the paper is accepted.