

1 We would like to thank the reviewers for their valuable comments. We first address the common criticisms, then turn to
2 each specific comments in what follows.

3 **Missing relevant work from the scheduling literature:** A common criticism from multiple reviewers is the lack of
4 mentioning about the relationship of MAXREWARD with scheduling problems in the paper. Indeed, there is a strong
5 connection between MAXREWARD and the interval scheduling problems. We have removed the description of this
6 connection from the submitted version mainly due to lack of space (also, we decided to prefer the other related work
7 and thus kept them instead in the paper to comply with the previous blocking bandit papers). We sincerely apologise for
8 this mistake and will add it back to our paper in the next version. This connection is described below in more detail:

9 The MAXREWARD problem belongs to the class of fixed interval scheduling problems with arbitrary weight values,
10 no preemption, and machine dependent processing time (see e.g., Kolen *et al.* 2007 for a comprehensive survey). This
11 is one of the most general, and thus, hardest versions of the fixed interval scheduling literature (see, e.g., Kovalyov,
12 Ng & Cheng 2007 for more details). In particular, MAXREWARD is a special case of this setting where for each
13 task, the starting point of the feasible processing interval is equal to the arrival time. Note that to date, provable
14 performance guarantees for fixed interval scheduling problems with arbitrary weight values only exist in offline, online
15 but preemptive, or settings with some special uniformity assumptions (Erleback & Spieksma 2000, Miyazawa &
16 Erleback 2004, Bender *et al.* 2017, Yu & Jacobson 2020). Therefore, to our best knowledge, *Theorem 2 in our paper is*
17 *the first result which provides provable approximation ratio for a deterministic algorithm in an online non-preemptive*
18 *setting. Note that with some modifications, our proof can also be extended to the general online non-preemptive setting,*
19 *i.e., online interval scheduling with arbitrary weight values, no preemption, and machine dependent processing time.*

20 **R1. Re: the presence of the reward of the Greedy algorithm in the approximation guarantee is not desirable:** Indeed, we
21 can remove the dependence on the performance of the online greedy algorithm in the approximation ratio as suggested
22 by the reviewer. For example, when $D \in O(1)$, we have $r(\pi^+) \in \Omega(T)$. Therefore, for settings with $B_T = o(T)$ we
23 get constant approximation ratio. Note that we also mentioned this in line 208. The reason we still used the form
24 described in Theorem 2 is to provide a convenient way to compare the performance of the online greedy with the
25 proposed bandit algorithm (see Appendix E for more details). We will update our paper to reflect this comment.

26 **Re: the bandit version's approximation guarantee is much weaker than the offline version when the delays are not big,**
27 **and the path variance is small:** This is indeed unavoidable. For example, consider the case of $D = 1$ for all the arms
28 and time steps (i.e., there is no blocking). In this scenario, it is easy to see that online greedy becomes optimal. On the
29 other hand, it is also known that in this case, the regret lower bound of bandit algorithms (against the optimal solution)
30 is $\Theta(\sqrt{TB})$ (see, e.g., Auer *et al.* 2002, Cesa-Bianchi & Lugosi 2006, Lattimore & Szepesvári 2019).

31 **Re: keeping track of the rewards during each phase when B_T is small and the phase length Δ_T is long:** This is indeed
32 a good idea, as when $D = 1$ (i.e., there is no blocking), Optimistic Mirror Descent (OMD) works with this insight and
33 typically gives the best B_T dependent bound (Wei & Luo 2018). However, OMD requires maintaining a probability
34 distribution over all the arms and this is not possible in our setting because of arbitrary blockings. B_T measures the
35 change in reward over consecutive rewards, but tracking such a change is not possible in a round if an arm is blocked.

36 **R2. Re: The hardness result for the offline problem with small blocking values:** We can easily extend our current proof
37 to the case of $T \gg D$. In particular, Let $T_0 = n + m = D$. We use the same proof in the paper but replace T with T_0 .
38 Now assume that $T \gg T_0$ (and thus, $T \gg D$). For any $T_0 < t \leq T$, we set the rewards to be 0 and blocks = 1 for
39 all the arms. It is still true that the optimal solution of this instance is linked to the solution of the original 3-SAT.

40 **Re: Whether the $O(\max \text{blocking length})$ performance gap is necessary:** We would like to highlight that there are 2
41 performance gap results in our paper: (i) The approximation ratio between the online greedy and that of the offline
42 optimal, and (ii) the regret between the bandit setting and the online greedy algorithm. For the latter, after the submission
43 of the paper we have managed to derive a general lower bound of $\Theta(\sqrt{BDT})$ (to prove this we reduced the problem of
44 combinatorial bandits with limited changes to our setting). Thus, the dependence of the regret bound on $\Theta(\sqrt{D})$ is
45 necessary. For the approximation ratio of the online greedy, it is true that we do not know whether our result is tight.
46 Therefore, it remains future work to investigate this case.

47 **R3. Re: more comprehensive numerical analysis needed:** We indeed only focus on the theoretical analysis of the
48 blocking bandit model. The numerical results in Appendix E is only for supporting the theoretical comparison between
49 Greedy-BAA and RGA. In particular, Eqs (19) and (20) from Appendix E show that Greedy-BAA is significantly better
50 than RGA when B_T is small (i.e., the regret bound of RGA is $O(\sqrt{T/B_T})$ -time larger). Hence the choice of $B_T = 3$.

51 **R4. Re: It seems like the main idea follows the standard reduction from bandit to full feedback with some non-trivial**
52 **adaptation:** We agree with the reviewer that the theoretical analysis of the bandit part is a non-trivial adaptation of
53 known techniques. However, we believe that this part still has its merits, as it provides a neat analysis for a new
54 and interesting bandit problem, laying the foundation for other adversarial blocking bandit models (e.g., contextual,
55 combinatorial, etc). This, combined with the other contributions of the paper, make our findings novel.