

1 We would firstly like to thank the reviewers for their time. We are particularly excited to see that even the reviewers  
 2 were inspired to propose a variety of extensions and improvements in their feedback, which shows the interest this  
 3 paper may generate at NeurIPS. In addition, we are pleased to see our algorithm is also capable of producing diverse  
 4 reviews. Given the green field nature of this project, we have some additional insights to provide since the submission.

5 **New RL experiments** We extended our RL experiments to the approximate  
 6 setting where gradients are computed using samples. We use an Actor-Critic  
 7 algorithm with a tabular policy, and compute Hessians using the DiCE oper-  
 8 ator (Foerster, 2018). The results show that RR works not only in the exact  
 9 setting but also when gradients are approximate. We believe this is a key step  
 10 towards eventually using RR for deep RL. We believe these results improve  
 11 the potential scalability of our approach, and will be included in the CRC.  
 12 Below we address individual comments in more detail:

13 **R1: Saddle vs local maximum** When we use the word ‘saddle’ we mean a stationary point with at least one negative  
 14 curvature direction, which includes maxima. **method ..not clearly defined .. even in authors’ minds.** We provide a  
 15 method section, multiple instances of pseudo code and implementations that closely match the pseudo code.

16 **R2: computation of the Hessian spectrum should be  $O(m^3)$ ..requires a spectral computation EACH**  
 17 **timestep..complexity analysis** We addressed this in the section labeled *Approximate Ridge Riding* There, we for-  
 18 mulated a version of RR that only requires Hessian-Vector products, which can be computed with  $O(m)$  complexity  
 19 in modern auto-diff frameworks. As explained, we also use an iterative process for updating the EV at each timestep  
 20 rather than recomputing it. The overall complexity will depend on the search method being used, but each solution will  
 21 required  $O(m) * O(N)$  compute, where  $N$  is the number of update steps. The memory is also dependent on the search  
 22 method, but will be  $O(m)$  for depth-first. **Theorem 1 assumption.** One can use Hessian-Vector products to compute  
 23  $\langle \nabla L(\theta), e_i(\theta) \rangle$  and estimate  $\gamma$  at any  $\theta$ . This can be used to set the learning rate. **minima not better than SGD.** We  
 24 show in both the zero-shot coordination problem and the out-of-distribution that RR can obtain better solutions than  
 25 SGD. Clearly though, in general this will be problem specific and all we can do is provide a method that can obtain more  
 26 diverse solutions. **cannot see how symmetry and equivalence relate to algorithm.** This is exploited and described  
 27 in the zero-shot coordination setting and in the out-of-distribution part. In general symmetries can be used to make the  
 28 search more efficient by only exploring one EV from each equivalence group.

29 **R3: Many thanks for the encouraging, insightful and positive review! ChooseFromArchive** The best way to search is  
 30 problem dependent, so we specify ChooseFromArchive separately in the method sections for each of our applications  
 31 and extensions of RR. **Many pre-print cited** We apologize. That there are 18 papers in the paper which look like  
 32 ‘pre-prints’ is an artifact of us using the default Google Scholar bibtext. Out for these 18, 3 are journal papers, 9 are  
 33 top-tier conference papers, and only 6 are actual pre-prints. Of those, 4 are from 2020, one is the Tensorflow paper  
 34 with >5k citations, and the last is the well-known and relevant MAP-elite algorithm. We will correct the citations in the  
 35 Camera Ready Copy (CRC).

36 **R7: Thank you for your interesting comments. We are glad you**  
 37 appreciate the novelty of our work in the ZS setting and note the  
 38 strength of the diversity in RL experiments. Regarding **RR not**  
 39 **working “in generality”**, we feel this is a high bar for any algorithm.  
 40 While we show that our algorithm is applicable and useful in a wide  
 41 array of diverse settings, we clearly can’t promise that it will find  
 42 all solutions in all settings (there is probably an impossibility result  
 43 somewhere to be written down here). **ridges vs. random directions**  
 44 We tried to address this in Fig 2 (in the paper) with a baseline that  
 45 follows random (unit) vectors instead of EVs (*Rand. Ridge*). To  
 46 evaluate your proposal, we include two additional baselines: (1)  
 47 following ridges, but not updating them (*Fixed-EV*). (2) following  
 48 random unit vectors with *positive ascent direction* (*Rand-Ridge+*),  
 49 and compare vs. Ridge Riding. We ran these ablations both on the RL experiment (exact RR) and on MNIST, where we  
 50 used a fixed budget hyperparameter search for approximate RR and the ablations. As shown in Fig 2, RR on MNIST  
 51 significantly outperforms all ablations. Fixed-EVs obtain a top accuracy of a linear classifier (92%), compared to the  
 52 98% obtained by RR. In contrast, none of the suggestions using random directions exceed 30%. In the low dimensional  
 53 RL example, Fixed-EVs obtains competitive performance. This clearly illustrates the importance of following EVs  
 54 rather than random directions. We furthermore observe all differences to be more pronounced in MNIST, which is  
 55 intuitive since random search is known to scale poorly to high dimensional problems. We expect this effect to be even  
 56 more pronounced as Approximate RR is applied to harder and higher dimensional tasks in the future. We once again  
 57 thank the reviewers for these suggestions and will update the paper to include all plots shown here.

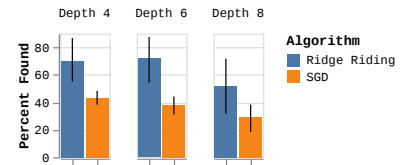


Figure 1: % solutions found per algorithm, by tree depth, each is randomly generated 10 times to produce error estimates shown.

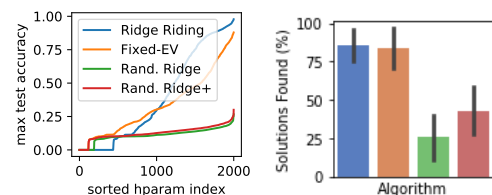


Figure 2: Ablations on ridge riding algorithm. Left: We perform a hyperparameter search for all methods on MNIST and show best performance found. Right: The same four methods for diversity in RL, with tree depth of 12, 5 seeds. Legend applies to both plots.