

1 We thank the three reviewers for their constructive comments. The following are our responses to reviewers’ comments.

2 —To Reviewer #1—

3 **Re. the notion of orthonormality:** When we designed our method, we followed the original forms of existing metric
 4 learning models and thus did not use the additional orthonormality constraints. Actually, metric learning aims to find
 5 embedding directions (see Fig. 1 in our paper) so that the resulting metric can faithfully preserve the intrinsic distances
 6 of data pairs. The directions with necessarily high variations for the subsequent classification are usually favored by
 7 many dimension reduction techniques such as PCA.

8 **Re. simplifying derivations and proofs:** As the reviewer suggested, in the final paper, we will try our best to simplify
 9 the derivations of gradients, and carefully expand the proofs to make them easier to understand.

10 **Re. the complexity, runtime, and code release:** The matrix multiplication complexities of Eq. (14) and Eq. (16) are
 11 $O(c^2hmd)$ and $O(Lchmd)$, respectively. Here h and d are the batch-size and data dimension correspondingly, and the
 12 constants c and L are independent of the size of datasets. Since the measurer line number m is always set to be smaller
 13 than d , the total complexity of our algorithm is $O(hd^2)$, which is the same as most of the baseline methods. The results
 14 of CPU hours (Core Duo 2.93GHz desktop with 16G RAM) on MVS dataset (10^5 training pairs and 10^4 test pairs) are
 15 presented in Table I, which show that our method requires comparable runtime with existing methods. We will release
 16 the code if this paper is accepted.

Table I: Runtime comparisons.

Methods	Training	Test
LMNN	2.35h	0.12h
ITML	1.96h	0.12h
DDML	3.65h	0.18h
PML	1.92h	0.15h
ODML	2.12h	0.12h
BDML	2.69h	0.12h
CDML	2.59h	0.16h

Table II: Classification error rates (%) (lower is better) and verification AUC values (higher is better) of compared methods.

Methods	Classification Tasks						Verification Tasks		
	Letter	Autmpg	Australia	Glass	Balance	Segment	Pub.	LFW	MVS
Npairs	4.32±0.51●	25.94±3.64●	16.32±0.12●	27.29±0.24●	9.09±0.12●	7.13±2.32●	90.1	87.9	73.7
Angular	3.55±0.61●	23.24±0.73●	15.32±2.56	28.12±0.23●	8.19±0.64●	6.19±3.64●	91.6	88.8	72.4
DAML	3.21±0.66●	22.23±0.61●	17.09±1.14●	24.12±3.54	9.03±0.64●	4.03±0.89●	91.5	88.1	76.6
Hard-Aware	3.11±0.23●	22.92±1.14●	16.32±1.14●	22.09±5.64	8.14±1.02	5.24±2.65●	91.9	88.5	73.2
CDML	2.09±0.64	15.32±6.11	12.22±2.54	22.12±4.64	5.01±2.64	1.23±0.32	92.4	89.1	77.1

17 —To Reviewer #2—

18 **Re. the interpretation should be regarded as a good motivation:** Thanks for your suggestions. We will modify our
 19 claim on interpretation (*i.e.*, Line 101) from the viewpoint of motivation. “which might be more intuitive than the
 20 previous interpretations.” → “which offers a clear way to handle the nonlinear data with geometric structures.”

21 **Re. more recent baselines and DDML training details:** As the reviewer suggested, we add new experiments for
 22 comparing the baseline methods “Npairs Loss” and “Angular Loss” reported in “Making Classification Competitive
 23 for Deep Metric Learning”(arXiv 2018, recommended by the reviewer). We also add two latest baselines “Deep
 24 Asymmetric Metric Learning(DAML) via Rich Relationship Mining”(CVPR 2019) and “Hardness-Aware Deep Metric
 25 Learning”(CVPR 2019) for further comparisons. The six classification datasets and three verification datasets in our
 26 paper are used here. Table II lists the error rates on classification tasks (“●” denotes a significantly better result at the
 27 significance level 0.05) and AUC values on verification tasks for various methods. Obviously, our CDML outperforms
 28 the recent baselines in most cases. We believe that the above new results further improve the fairness and sufficiency of
 29 our experiments, and we will duly add them in our final paper. For the training of DDML details, the regularization
 30 parameter λ was tuned via searching the grid $\{10^{-2}, 10^{-1}, 1, 10, 10^2\}$ by observing the model performance on validation
 31 set. Other configurations such as network architectures, weight initializations, and SGD-related parameters were set as
 32 recommended by the authors of “Discriminative Deep Metric Learning for Face Verification in the Wild”(CVPR 2014).

33 —To Reviewer #3—

34 **Re. the solution and Theorem 2/3:** The theoretical analyses on generalization bound usually focus on the ideal case
 35 when the globally optimal solution is obtained, although the models are nonconvex such as “Learning Latent Space
 36 Models with Angular Constraints”(ICML 2017) and “Fast Generalization Error Bound of Deep Learning from a Kernel
 37 Perspective”(ICML 2018). We thus follow such common practice and also discuss the ideal case in our theoretical
 38 analysis. The globally optimal solution might not be acquired by our method practically due to the non-convexity of
 39 objective function, and this practical phenomenon is also observed in above prior works.

40 **Re. discussing tensor \mathcal{A} and function $B(\lambda)$:** The tensor \mathcal{A} is predefined to smooth and stabilize the learning of
 41 polynomial coefficients. We can treat it as a constant which restricts the high variations of the learning parameter
 42 \mathcal{M} within a small hypothesis space. In our experiments, \mathcal{A} is simply fixed to $\mathbf{0}$, *i.e.*, using the original Frobenius-
 43 norm regularizer. For the function $B(\lambda)$, its expression has been shown in Eq. (B.14) in supplemental materials as
 44 $B(\lambda) = 2\mathbb{E}_{\mathcal{X}, \mathcal{Z}}(\sup_{\mathcal{M} \in \mathcal{F}(\lambda)} \bar{\epsilon}_{\mathcal{Z}}(\mathcal{M}) - \bar{\epsilon}_{\mathcal{X}}(\mathcal{M})) / \mathbb{E}_{\mathcal{X}, \mathcal{Z}}(\sup_{\mathcal{M} \in \mathbb{R}^{m \times d \times c}} \bar{\epsilon}_{\mathcal{Z}}(\mathcal{M}) - \bar{\epsilon}_{\mathcal{X}}(\mathcal{M}))$. This expression reveals that
 45 when the regularization parameter λ increases, the hypothesis space $\mathcal{F}(\lambda)$ shrinks, so the numerator in the above
 46 expression decreases (the denominator does not change as it is irrelevant to λ), which further leads to a smaller $B(\lambda)$
 47 and a tighter upper bound. We will add the above discussions in the final paper.

48 **Re. declaration for “supervised metric learning”:** Thanks. We will carefully declare that our paper focuses on
 49 supervised metric learning in the Introduction section.