A Unifying LIME and Shapley value to Dialogue Response Generation

A.1 Learning based Local Approximation Explanation

Taking the prediction of each time step in sequence generation as classification over a lexicon, we can define the loss function as mean square error, the \( u(x) = x, z = h(\tilde{x}) = \{ \mathbb{1} (\tilde{x} = x_i) \}_{i=1}^{|x|} \) and the gain function \( g \) as

\[
g(y_j|\tilde{x}, y_{<j}) = P_\theta(y_j|\tilde{x}, y_{<j})
\]

Then LIME can be cast exactly as Equation (6)

\[
\Phi_j = \arg \min_{\Phi_j} E_{P(z)}(P_\theta(y_j|\tilde{x}, y_{<j}) - \Phi_j^T z)^2, \forall j
\]

A.2 Game Theory based Attribution Methods

We first define the gain function is

\[
g(y_j|\tilde{x}, y_{<j})_i = P_\theta(y_j|\tilde{x} \cup i, y_{<j}) - P_\theta(y_j|\tilde{x}, y_{<j}), \text{if } i \notin \tilde{x} \text{ else } g(y_j|\tilde{x}, y_{<j})_i = 0
\]

The \( Z = h(\tilde{x}) \in \mathbb{R}^{M \times M} \) is defined to be a diagonal matrix with the diagonal being

\[
Z_{ii} = 1, \text{if } i \notin \tilde{x} \text{ else } 0 = 0
\]

With the loss function being L2-norm, we can see the equation is exactly the same as the Equation (6)

\[
\Phi_j = \arg \min_{\Phi_j} E_{P(z)}||g(y_j|\tilde{x}, y_{<j}) - \Phi_j^T Z||_2
\]

B The proof of Properties

Property 1: unbiased approximation To ensure the explanation model \( \Phi \) explains the benefits of picking the sentence \( y \), the summation of all elements in \( \Phi \) should approximate the difference between the certainty of \( y \) given \( x \) and without \( x \) (the language modeling of \( y \)).

\[
\sum_j \sum_i \Phi_{ij} \approx \log P(y|x) - \log P(y)
\]

proof:

\[
\sum_j \sum_i \Phi_{ij} = \sum_j \sum_{i \in x} E_{x \in S \setminus i}[\log P(y_j|\tilde{x} \cup \{ x_i \}) - \log P(y_j|\tilde{x})]
\]

\[
= \sum_j \sum_i E \log P(y_j|\tilde{x} \cup \{ x_i \}) - \sum_i E \log P(y_j|\tilde{x})
\]

\[
\approx \sum_j \sum_{i \in x} P(\tilde{x}) \log P(y_j|\tilde{x} \cup \{ x_i \}) - \sum_i P(\tilde{x}) \log P(y_j|\tilde{x})
\]

\[
= \sum_j [\log P(y_j|x, y_{<j}) - \log P(y_j|\emptyset, y_{<j})]
\]

\[
= \log P(y|x) - \log P(y)
\]

Property 2: consistency To ensure the explanation model \( \Phi \) consistently explains different generation steps \( j \), given a distance function if

\[
D(P_\theta(y_j|\tilde{x}, y_{<j}), P_\theta(y_j|\tilde{x} \cup \{ x_i \}, y_{<j})) > D(P_\theta(y_{j'}|\tilde{x}, y_{<j'}'), P_\theta(y_{j'}|\tilde{x} \cup \{ x_i \}, y_{<j'})), \forall j', \forall x' \in x \setminus \{ x_i \}
\]

then \( \Phi_{ij} > \Phi_{ij'} \).

When taking the distance function as the difference between log-probabilities, we can prove that Equation (13) has this property by reducing the property to be the consistency property of Shapley value [27]. Prior work [52] has shown that the assumed prior distribution of Shapley value is the only one that satisfies this monotonicity.
Property 3: cause identification  To ensure that the explanation model sorts different input features by their importance to the results, if

\[ g(y_j|\tilde{x} \cup \{x_i\}) > g(y_j|\tilde{x} \cup \{x'_i\}), \forall \tilde{x} \in \mathcal{X} \setminus \{x_i, x'_i\} \]  \hspace{1cm} (28)

then \( \Phi_{ij} > \Phi_{i'j} \).

The unified formulation (Equation 6) is to minimize the difference between \( \phi \) and the gain function \( g \). If an optimized \( \phi^* \) exists, \( g \) can be written as \( g(y_j|\tilde{x} \cap \iota) = \phi^*_j(\tilde{z} + e_{i=1}) \). Therefore the inequality \( (28) \) can be derived as:

\[ \begin{align*}
\Phi_{ij} &> \Phi_{i'j} \\
\Leftrightarrow & \phi^*_j(e_i) > \phi^*_j(e_{i'}) \\
\Leftrightarrow & \phi^*_{ij} > \phi^*_{i'j}
\end{align*} \]  \hspace{1cm} (29)

Since Shapley_log of LERG is a variation to express the optimized \( \phi \), the method adheres to Property 3 without assumptions.

C  Experiment Details

For all methods, we sample 1000 perturbations of input. Also, to reduce the effect of off-manifold perturbations, we perturb input with at most half the features are changed. After three runs with random initialization for each method, the variances of the results are at most 0.001 and do not affect the trend. Our code is available at https://github.com/Pascalson/LERG.

All methods can be run on single GPU. We run them on one TITAN RTX.

D  User Study Details

Figure 5 are the screenshots of our instruction and question presented to workers on Amazon Mechanical Turk. We paid workers an estimated hourly wage 18 usd. For every 5 questions, the estimated spent time is about 30 seconds and the worker was paid 0.15 usd.

E  More Experiments

Beyond our main experiments on Dailydialog [25], we further take a look into how Shapley value and LERG_S work on personalized conversation and abstractive summarization. We specifically use datasets PersonChat [54] for the personalized conversation task and XSum [30] for abstractive summarization. We fine-tuned a GPT model on PersonChat as [47] and directly used the BART model [23] that has been pretrained on XSum. The
Similar to the results of our main experiments, Figure 6(a) and 6(c) show similar trend of increased \( PPL_{CR} \) with a higher removal ratio, with LERG_S consistently performing better. Further, the \( PPL_A \) also shows a similar trend to the main experiments, with the perplexity decreasing until some ratio and subsequently increase. Interestingly, the lowest ratio occurs earlier compared to the experiments on DailyDialog. This phenomenon can mean that the number of key terms in the input text of PersonaChat and XSum are less than the one of DailyDialog. Besides this ratio, we observe that LERG_S consistently has lower perplexity.

**Implementation Details** Throughout the preliminary study of PersonaChat, we specifically investigate the influence of dialogue history to the response and ignore profiles in the input. For XSum, we only run explanation methods on documents containing less than 256 tokens and responses with greater than 30 tokens, therefore, the perplexity is lower than the one reported in [23].

**F Discussion of Local Explanation with Phrase-level Input Features**

We tried two methods of phrase-level experiments. In the first approach, we used parsed phrases, instead of tokens, as the \( x_i \) and \( y_j \) in the equations and obtained explanations through Algorithm 1. In the second approach, we used the token-level explanations and averaged the scores of tokens in the same phrase parsed by an off-the-shelf parser. In both cases, the trend of the performance was similar to token-level methods. However, we suppose that the basic unit of dialogues is hard to define. Therefore we choose tokens in this paper for that tokens can be flexibly bottom-up to different levels of units.