

1 We thank the reviewers for their careful and thoughtful reviews.

2 **Concerns about the time series experiments (R1, R2, R3)**

3 The reviewers pointed out that we did not use standard baselines; we agree the paper would be
4 strengthened by including them. Hence, we compared with Euclidean nearest neighbor (B1), dynamic
5 time warping with optimized (B2) and constant window width (B3), persistence scale-space kernel
6 on the Rips filtration (without density), (R), standard 1D persistence image (I) and landscapes (L) of
7 a weighted average of Rips and density, and the multiparameter kernel (MP-K), landscape (MP-L),
and image (MP-I). We show results for only a few datasets due to lack of space.

Dataset	B1	B2	B3	R	I	L	MP-K	MP-L	MP-I
GunPointOldVersusYoung	95.2	96.5	83.8	-	98.7	95.9	99.0	97.1	100.0
ProximalPhalanxOutlineCorrect	80.8	79.0	78.4	78.4	67.4	72.5	78.7	78.7	81.8
ECG200	88.0	88.0	77.0	67.0	68.0	68.0	77.0	74.0	83.0
Plane	96.2	100.0	100.0	82.9	64.8	82.9	92.4	84.8	97.1
SyntheticControl	88.0	98.3	99.3	50.0	45.7	44.0	50.7	60.3	56.3

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9 We interpret this table to indicate that multiparameter persistence is a competitive option for this
10 problem, and our method is the best of the persistence-based approaches. However, our view is that
11 the real virtue of this method comes in situations such as the immunofluorescence images experiment.

12 **Standard deviations** (std) on the train set for these results when cross-validating were on the order
13 of 0.05. There is no std for the test set since we used suggested train / test splits. **Computation**
14 **times** for MP-I on these tasks averaged around 350 seconds; this was 3-4 times faster than MP-L and
15 around 30-50 times faster than MP-K. The other summaries based on 1D persistence had running
16 times similar to MP-I. **Size of feature space** It is correct that we worked with 10x10 and 50x50
17 images. We cross-validated all of the methods with up to 2,500 features, to ensure fair comparison;
18 hence we do not think the size of the feature space accounts for performance improvements.

19 **Stability with respect to matching (R1, R2, R3)**

20 We agree with the reviewers that there is a disconnect between the theory and stability in practice.
21 We will expand the discussion of this in the revision.

22 **Perturbing the lines** We experimented with random perturbations of the lines selected (both by
23 randomly shifting the angles and making them closer and further apart). Accuracies degraded slowly
24 in the size of the perturbations. For instance, when perturbing the line endpoints with noise whose
25 amplitude was up to 10 times the distance between the lines, the mean accuracy of ECG200 and
26 GunPoint went down by only 2-3%, with std around 0.02. **Matching instability** We never detected
27 this in practice in any of the examples we ran, although it is easy to create synthetic examples
28 exhibiting it. We will detail how to detect it (by comparing with bottleneck matchings) in the revision.

29 **Extension to multiparameter persistence (R2)**

30 We agree with R2 that extending the MP-I to multiparameter persistence is potentially subtle, and
31 requires discussion of the choice of lines. For example, in R^3 , one would sweep the 3D space
32 with planes that all intersect on a given line. Since each plane would itself be swept with lines, 2D
33 summands can be computed in each plane, and then connected through the common line to generate
34 3D summands. The stability result generalizes to this situation with a different geometric base case.

35 **Clarity (R1, R2, R3)**

36 All reviewers made very useful comments about how to improve clarity of the paper, which we
37 will incorporate. We also thank R1 for the writing comments and reference works. We answer
38 their questions here. **DTM**: we didn't study stability w.r.t. the DTM parameters but this is a very
39 interesting question to look at. **Bounding rectangle** refers to the rectangle given by the minima and
40 maxima of both filtrations. **Fig 2**: n should be replaced by N . **Lines**: The reason why N is not fixed
41 for lines with same slope is because we implemented it that way. There is no theoretical obstruction
42 for this though. $f|_l$ is indeed an abuse of notation. **Def 3.3**: n should be p and a, b, c, d should satisfy
43 $a \leq b, c \leq d$. **Fig 4** was generated with lines of same slope. Sets of large bars indicate topological
44 features that are persistent in both filtrations: in our case, circles with large diameters that are made
45 of points with large density. Smaller loops would generate bars with smaller lengths for at least one
46 filtration. Difference between a big loop and many small loops shows in the decomposition, but can
47 be missed in MP-I since all the Gaussian functions (corresponding to the sets of bars) are summed.