

Table A: FID on CIFAR10. \dagger means averaged by 5 runs. Methods with \ddagger use comparable networks.

Method	FID \downarrow	FID-ES \downarrow
Flow-CE [1*]	37.30	-
VAE-EBLVM[2*]	30.1	-
MDSM \ddagger [34]	-	31.7
MDSM \ddagger (our code)	39.12	30.19 \pm 2.60 \dagger
BiMDSM \ddagger (20)	34.55	26.62 \pm 1.52 \dagger
BiMDSM \ddagger (50)	38.82	29.43 \pm 2.76 \dagger
BiMDSM \ddagger (100)	-	26.90 \pm 2.14 \dagger

Table B: Test log-likelihood (LL) results on Frey face. We use 2,000 chain samples in AIS.

Method	LL \uparrow
DSM	129.23
BiDSM ($N=0$)	107.59
BiDSM ($N=1$)	110.65
BiDSM ($N=5$)	124.00
BiDSM ($N=10$)	125.72

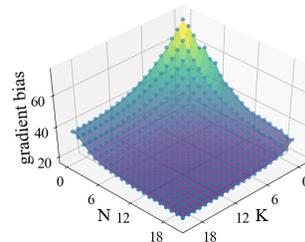


Figure A: The gradient bias (i.e., the left hand side of Thm. 2) w.r.t. N and K in GRBM on Frey face.

1 We thank all reviewers for their valuable comments. We **update the FID results in Tab. A, validate Thm.2 in**
 2 **Fig. A, add AIS results in Tab. B, add three baselines (VNCE [42], [1*] and [2*]),** and clarify other issues (e.g.,
 3 computation time). Below, we first address the common concerns and then answer the detailed questions.

4 **Common concern (CC) 1 from R#2&R#4 Validate Thm. 2:** In Fig. A, the gradient bias decays (approximately)
 5 exponentially w.r.t. N , as proved in Thm. 2. Besides, we find that as K increases from 0 to 20, $\|\phi^0 - \hat{\phi}^*\|$ decreases
 6 from 1.38 to 0.87. It leads to smaller bias (see Fig. A), which also agrees with Thm. 2. **CC2 from R#2&R#4&R#5**
 7 **Benefits of EBLVM:** First, introducing latent variables can improve the sample quality (w.r.t. FID) in a fair comparison.
 8 Indeed, we update Tab. 2 and obtain Tab. A, whose second column shows the FID with early stopping (ES) according
 9 to the results on 1,000 samples. As stated in L290, a similar protocol is adopted in MDSM [34]. We also implement
 10 MDSM in our code for a fair comparison. The reproduced MDSM is slightly better than the original paper [34] and
 11 serves as a stronger baseline. Our result outperforms MDSM and [1*]. We mention that [2*] generate samples from a
 12 VAE instead of an EBM and is less comparable. Second, the deep EBLVM is not suitable for conditional generation
 13 because $p(v|h; \theta)$ is multimodal. The results (Fig.4) and analysis are shown in Appendix C.2.2. We expect that the
 14 model can serve as a benchmark and inspire new model design. **CC3 from R#3&R#4 Computation time:** The time
 15 complexity per gradient estimate is $O(N+K)$. However, empirically, we don't need arbitrarily large N and K . Indeed,
 16 in the default setting, the training time per 100 iterations is 8.61s for BiDSM, 1.59s for CD-5, 4.36s for VNCE, 1.33s for
 17 DSM in GRBM on Frey face. The training time of 300,000 iterations is 48h for BiMDSM and 32h for MDSM in deep
 18 EBLVM on CIFAR10 (see L118 in Appendix B.2). Thus, BiSM can learn general EBLVMs without a prohibitive cost.

19 **To R#2. Typos:** We'll correct it in the final version. **Strongly convex assumption in Thm. 2:** Currently the assumption
 20 is necessary. **Dependence on the batch size:** An infinite batch size is not necessary. Actually, the constants (A, B, C
 21 and κ) and the learning rate α can be made independent of the batch size by applying assumptions 2 and 3 in Thm.
 22 2 to $\mathbb{E}_{q(h|v; \phi)} \mathcal{F}(\dots)$ (Eqn. (8)) and $\mathcal{D}(\dots)$ (Eqn. (9)) instead of $\hat{\mathcal{J}}_{Bi}$ and $\hat{\mathcal{G}}$. **Update ϕ for K times on the same**
 23 **minibatch:** It is a special design. According to Thm. 2, we should minimize $\|\phi^0 - \hat{\phi}^*\|$, where $\hat{\phi}^*$ is optimal on
 24 a given minibatch. We update ϕ multiple times on the same minibatch to obtain ϕ^0 that approximates $\hat{\phi}^*$. We'll
 25 make it clearer. **Validating Thm. 2 and ablation study:** See the common concern 1. We'll add the ablation study
 26 of K . **Practical usefulness:** See the common concern 2. **CelebA 128x128:** We obtain promising generation results
 27 on CelebA 64x64 and are working on 128x128 data. We'll include the results. **Noise annealing on the images:** It is
 28 necessary. Indeed, MDSM uses the annealed noise in its objective (Eqn. (5)). **Recent work:** Thanks. We'll discuss it.

29 **To R#3. Compare to [1*]:** Thanks, we compare to [1*] in Tab. A. **Higher dimension of h is worse:** We add a new
 30 experiment with h dimension (d_h) of 100 in Tab. A, which is comparable to $d_h = 20$. The relatively worse results
 31 of $d_h = 50$ may be caused by the variance of training on different initial seeds. **Unstable learning:** The lower level
 32 optimization can be slightly unstable because the distribution of EBLVM is moving during training. The higher level
 33 optimization is stable. We'll plot it in the final version.

34 **To R#4. Compare to VNCE [42]:** We implement VNCE. On the toy data, its log likelihood is 0.303 nats, which is
 35 worse than 0.319 nats of BiDSM. We'll add the curve of VNCE to Fig. 2 in the final version. **Missing reference:**
 36 Thanks. We'll discuss this work in the final version. **Motivation of deep EBLVM:** See the common concern 2.
 37 **Likelihood estimate:** See Tab. B. BiDSM gets closed to DSM as N increases and $N \geq 5$ is sufficient. **Trades-offs**
 38 **and future work:** Taking less than twice computation time of the regular SM (see common concern 3), BiSM can learn
 39 deep EBLVMs. We'll discuss the future work in the final version. **Inference model:** Thanks. The inference model
 40 is similar to the one used in VAE, as described in Appendix B.1 and B.2 (also see the code in the anonymous link in
 41 Page 6). We will add more details in the main text. **Correctness:** See common concern 1. **Clarity:** The algorithm is
 42 consistent to what you believe and we'll improve the clarity.

43 **To R#5. Experimental results and compare to [2*]:** We use the widely adopted FID (Tab. A) metric for evaluation
 44 and compare to strong baselines [34][1*][2*]. Our updated results outperform baselines with comparable architectures
 45 (see common concern 2). **Missing references:** We will include the missing references mentioned in the comments.
 46 [1*] Flow contrastive estimation of EBMs. [2*] Joint Training of Variational Auto-Encoder and Latent EBM.