
Rethinking the CSC Model for Natural Images

Supplementary Material

Anonymous Author(s)

Affiliation

Address

email

- 1 This document contains supplementary material for “Rethinking the CSC Model for Natural Images”
- 2 paper, submitted to NeurIPS 2019.

3 1 Strided CSC Results

- 4 In Table 1 we provide a per-image detailed comparison for the Set12 dataset (see Figure 1) between
- 5 the PA method and the strided CSC concept that was introduced in the paper under Section 4. Note
- 6 that this experiment corresponds to a fixed (not learned) twice redundant DCT dictionary.

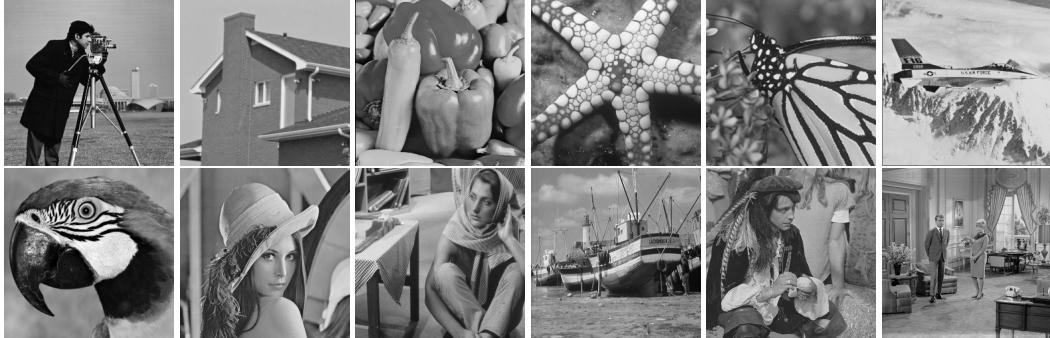


Figure 1: The Set12 images.

7 2 CSCNet Details

8 2.1 Parameter Initialization

- 9 Since the CSCNet architecture imitates the operation of the ISTA algorithm, we initialize its parame-
- 10 ters such that each layer will indeed follow an ISTA iteration. To do so, we first initialize a random
- 11 set of filters that are similar to a CSC dictionary, i.e. a deconvolution operator \mathbf{D} and normalize it
- 12 by $\sqrt{\sigma_{\max}(\mathbf{D}^T \mathbf{D})}$, where the largest eigenvalue is found using the power method, implemented to
- 13 operate on convolutional operators. Once the operator is normalized, we initialize the parameters of
- 14 the network as follows: $\mathbf{A} = \mathbf{D}^T$, $\mathbf{B} = \mathbf{D}$ and $\mathbf{C} = \mathbf{D}$. For the soft thresholding operator, we set
- 15 its thresholds vector τ to a constant vector with the value 0.01, which is equivalent to setting the λ
- 16 parameter of the original Lagrangian problem to $\lambda = 0.01$ which has been empirically found to work
- 17 well. In the iterative process itself, we assume that \mathbf{T}_0 , i.e. the initial sparse representation, is zero.

18 **2.2 Training CSCNet**

19 To train this model we use the Pytorch framework [1] installed on a standard PC containing an Intel(R)
20 Core(TM) i7-6900K CPU and a single Nvidia GeForce GTX 1080Ti. Training a model on this setup
21 takes approximately 14 hours. The code used to train the model, alongside the trained models
22 that were used in this paper are publicly available at <https://anonymous.4open.science/r/a550eeb5-942e-4ffc-b75d-f0fb3d58785f/>.
23

24 **2.3 Hyper-parameters Comparison**

25 In this subsection we explore the effect of various parameters used in our model. Unless stated
26 specifically otherwise, in the following described experiments the standard deviation of the noise is
27 $\sigma = 25$, the filters used have a size of 11×11 , the stride chosen is $q = 8$ and we train for 250 epochs.
28 The BSD68 dataset is used to evaluate the performance of the various models.

29 The first hyper-parameter we consider is the size of the stride. The paper itself discusses the effect of
30 the size of the stride on the trained model. As presented in the paper, a small stride leads to highly
31 correlated filters reducing the performance of the model. On the other extreme, when the stride is too
32 large, the performance reduces due to the lack of sufficient overlap between the filters.

33 The next parameter we examine is the depth of the network, i.e. the number of LISTA iterations
34 used. Figure 2 demonstrates the effect of the depth of the network on the denoising performance.
35 As expected, a deeper network leads to higher PSNR results. That said, the improvement seems to
36 saturate at a certain depth. We chose a depth of 12 as a compromise between the performance of the
37 model and its training time.

38 Another parameter to consider is the size of the filters. Figure 3 demonstrates the performance of
39 various models trained with different filter sizes. From the figure we learn that increasing the size of
40 the filters improves the denoising performance of the trained models. That said, this also increases
41 the number of computations required to obtain an estimate, making the learning process much slower.
42 Training a model with filter size of 15×15 took approximately two days, while improving the
43 performance by a relatively small margin (0.06dB). Hence, in our reported results, we chose 11×11
44 for the size of the filters.

45 The last parameter we examine is the number of epochs. We trained our model with a filter size of
46 11×11 for 500 epochs, and demonstrate its denoising performance on the BSD68 test set during the
47 training phase in Figure 4. From the figure, it seems that one can improve the denoising results further
48 by continuing the training process, but only by an insignificant increase in performance. Therefore,
49 we have decided to stop the training process after 250 epochs, practically reaching convergence.

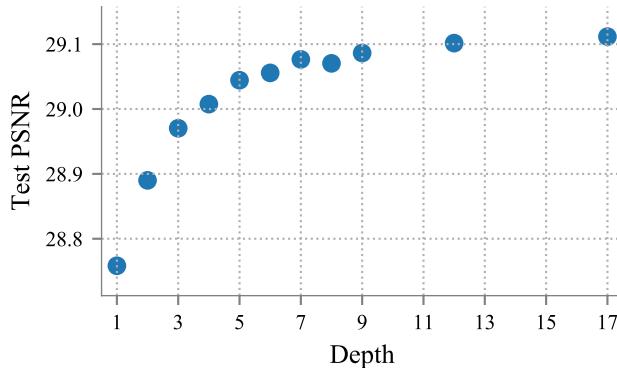


Figure 2: The effect of the depth of the CSCNet on its denoising performance.

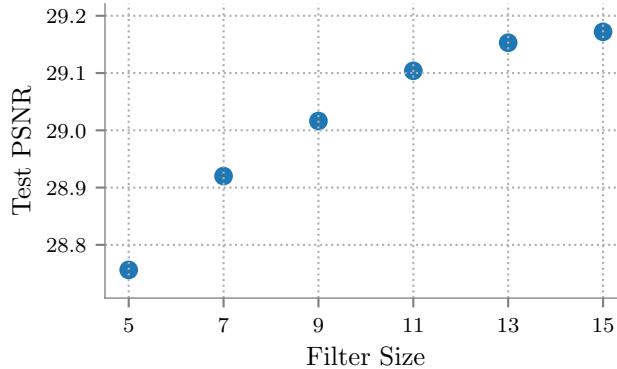


Figure 3: The effect of the size of the filters on the denoising performance of CSCNet.

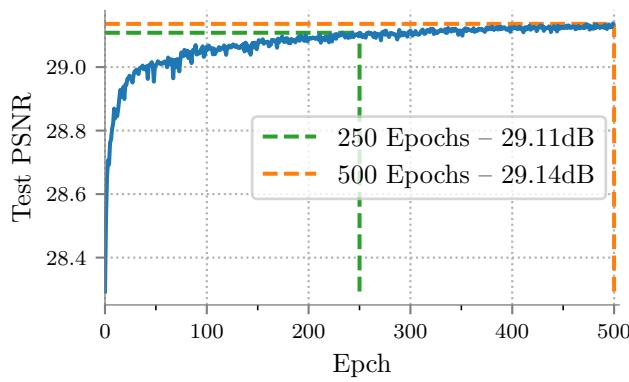


Figure 4: The convergence of the CSCNet model over the number of epochs.

50 2.4 Additional Results

51 Table 2 Shows the denoising performance of our proposed method, alongside other leading denoising
 52 algorithms on the Set12 dataset. Note that our method is indeed on par with current leading methods,
 53 especially when the energy of the noise is high.

54 References

- 55 [1] Adam Paszke, Sam Gross, Soumith Chintala, Gregory Chanan, Edward Yang, Zachary DeVito, Zeming Lin,
 56 Alban Desmaison, Luca Antiga, and Adam Lerer. Automatic differentiation in pytorch. 2017.

Table 1: Set12 denoising results (PSNR) using PA and CSC with various strides (q). CSC Results that surpass PA are marked in blue. Best results are bold.

Image	CSC											PA
	$q = 1$	$q = 2$	$q = 3$	$q = 4$	$q = 5$	$q = 6$	$q = 7$	$q = 8$	$q = 9$	$q = 10$		
	$\sigma = 15$											
C.man	28.47	28.73	29.40	30.00	30.36	30.54	30.63	30.71	30.77	30.80	30.66	
House	29.91	30.17	31.33	32.38	32.98	33.28	33.34	33.46	33.57	33.64	33.44	
Peppers	28.90	29.14	29.97	30.66	31.06	31.20	31.38	31.45	31.49	31.43	31.09	
Starfish	28.26	28.35	28.80	29.35	29.76	29.82	29.96	30.06	30.14	30.15	29.86	
Monarch	28.43	28.59	29.20	29.83	30.28	30.39	30.53	30.61	30.64	30.62	30.29	
Airplane	27.95	28.19	28.85	29.45	29.77	29.99	30.11	30.18	30.21	30.23	30.17	
Parrot	28.55	28.76	29.37	29.93	30.26	30.45	30.57	30.63	30.70	30.73	30.51	
Lena	30.17	30.76	31.87	32.66	33.11	33.24	33.34	33.46	33.52	33.50	33.12	
Barbara	29.60	30.10	30.92	31.56	32.00	32.08	32.15	32.27	32.30	32.26	31.90	
Boat	29.23	29.54	30.27	30.81	31.17	31.32	31.38	31.43	31.51	31.56	31.40	
Man	29.23	29.49	30.09	30.61	30.95	31.06	31.15	31.22	31.27	31.31	31.11	
Couple	29.18	29.37	30.05	30.63	30.97	31.11	31.18	31.23	31.26	31.30	31.17	
$\sigma = 25$												
C.man	25.19	25.45	26.24	26.99	27.44	27.75	27.87	27.98	28.10	28.18	28.09	
House	26.46	27.00	28.18	29.34	30.07	30.46	30.57	30.77	30.97	31.08	31.01	
Peppers	25.70	25.88	26.80	27.70	28.35	28.63	28.78	28.89	28.93	28.91	28.71	
Starfish	25.02	25.14	25.74	26.38	26.84	26.98	27.17	27.26	27.32	27.37	27.18	
Monarch	25.18	25.41	26.11	26.82	27.34	27.50	27.71	27.82	27.87	27.86	27.54	
Airplane	24.72	24.97	25.72	26.43	26.89	27.20	27.34	27.42	27.47	27.52	27.59	
Parrot	25.30	25.55	26.29	27.01	27.53	27.83	27.94	28.05	28.15	28.20	28.02	
Lena	26.95	27.54	28.78	29.73	30.41	30.66	30.80	30.97	31.07	31.09	30.74	
Barbara	26.31	26.83	27.70	28.46	29.06	29.28	29.43	29.58	29.66	29.64	29.32	
Boat	26.15	26.51	27.35	28.03	28.54	28.72	28.81	28.89	28.99	29.07	29.02	
Man	26.28	26.57	27.30	27.90	28.38	28.55	28.68	28.75	28.84	28.90	28.78	
Couple	26.18	26.39	27.11	27.79	28.27	28.46	28.54	28.62	28.68	28.78	28.73	
$\sigma = 50$												
C.man	20.83	21.00	21.98	22.85	23.63	24.13	24.34	24.53	24.72	24.88	24.80	
House	21.83	23.18	24.59	25.43	26.33	26.61	26.83	27.26	27.57	27.78	27.75	
Peppers	21.45	22.18	23.25	23.81	24.48	24.87	25.06	25.26	25.37	25.38	25.18	
Starfish	20.83	21.36	22.21	22.52	23.10	23.44	23.74	23.95	24.07	24.07	23.73	
Monarch	20.73	20.99	21.90	22.57	23.33	23.62	23.83	24.03	24.20	24.22	23.82	
Airplane	20.60	21.45	22.19	22.68	23.30	23.71	23.94	24.09	24.18	24.30	24.23	
Parrot	20.91	21.14	22.13	22.96	23.66	24.07	24.28	24.52	24.71	24.81	24.29	
Lena	22.48	23.40	24.87	25.76	26.53	26.91	27.09	27.41	27.65	27.75	27.47	
Barbara	21.87	22.41	23.48	24.31	24.96	25.35	25.53	25.77	25.98	26.06	25.61	
Boat	22.03	22.56	23.61	24.30	24.96	25.27	25.40	25.61	25.80	25.93	25.81	
Man	22.23	22.93	24.15	24.75	25.25	25.44	25.60	25.80	25.97	26.05	25.84	
Couple	22.13	22.71	23.65	24.06	24.67	24.93	25.02	25.23	25.40	25.54	25.36	
$\sigma = 75$												
C.man	18.26	19.00	20.05	20.67	21.35	21.96	22.28	22.56	22.81	23.00	22.95	
House	18.88	20.17	22.08	23.25	24.06	24.38	24.65	25.08	25.45	25.69	25.57	
Peppers	18.66	19.51	21.09	21.89	22.43	22.64	22.83	23.04	23.22	23.27	22.98	
Starfish	18.26	18.96	20.28	20.94	21.39	21.45	21.78	22.00	22.23	22.30	21.73	
Monarch	18.13	18.65	19.91	20.60	21.23	21.53	21.83	22.16	22.34	22.37	21.85	
Airplane	18.08	19.34	20.59	21.10	21.48	21.65	21.81	22.02	22.19	22.28	22.07	
Parrot	18.25	18.70	20.03	20.85	21.43	21.85	22.14	22.42	22.67	22.81	22.43	
Lena	19.72	20.51	22.21	23.46	24.26	24.71	24.87	25.25	25.64	25.86	25.33	
Barbara	19.20	19.66	20.75	21.74	22.49	23.00	23.13	23.39	23.69	23.90	23.25	
Boat	19.41	20.03	21.38	22.25	22.89	23.22	23.40	23.67	23.96	24.17	23.83	
Man	19.61	20.26	21.63	22.68	23.37	23.66	23.80	24.08	24.37	24.54	23.88	
Couple	19.47	20.17	21.45	22.27	22.78	22.96	23.10	23.31	23.56	23.74	23.48	

Table 2: Set12 denoising results (PSNR) comparison using various methods. The best and second-best results are highlighted in red and blue respectively.

Image	BM3D	WNNM	MLP	TNRD	DnCNN	FFDNet	CSCNet
$\sigma = 15$							
C.man	31.91	32.17	–	32.19	32.61	32.42	32.40
House	34.93	35.13	–	34.53	34.97	35.01	34.96
Peppers	32.69	32.99	–	33.04	33.30	33.10	33.19
Starfish	31.14	31.82	–	31.75	32.20	32.02	31.89
Monarch	31.85	32.71	–	32.56	33.09	32.77	32.78
Airplane	31.07	31.39	–	31.46	31.70	31.58	31.60
Parrot	31.37	31.62	–	31.63	31.83	31.77	31.86
Lena	34.26	34.27	–	34.24	34.62	34.63	34.44
Barbara	33.10	33.60	–	32.13	32.64	32.50	32.22
Boat	32.13	32.27	–	32.14	32.42	32.35	32.29
Man	31.92	32.11	–	32.23	32.46	32.40	32.31
Couple	32.10	32.17	–	32.11	32.47	32.45	32.31
Average	32.37	32.70	–	32.50	32.86	32.75	32.69
$\sigma = 25$							
C.man	29.45	29.64	29.61	29.72	30.18	30.06	29.95
House	32.85	33.22	32.56	32.53	33.06	33.27	33.07
Peppers	30.16	30.42	30.30	30.57	30.87	30.79	30.74
Starfish	28.56	29.03	28.82	29.02	29.41	29.33	29.02
Monarch	29.25	29.84	29.61	29.85	30.28	30.14	30.07
Airplane	28.42	28.69	28.82	28.88	29.13	29.05	28.98
Parrot	28.93	29.15	29.25	29.18	29.43	29.43	29.43
Lena	32.07	32.24	32.25	32.00	32.44	32.59	32.34
Barbara	30.71	31.24	29.54	29.41	30.00	29.98	29.36
Boat	29.90	30.03	29.97	29.91	30.21	30.23	30.11
Man	29.61	29.76	29.88	29.87	30.1	30.1	29.99
Couple	29.71	29.82	29.73	29.71	30.12	30.18	30.01
Average	29.97	30.26	30.03	30.06	30.43	30.43	30.26
$\sigma = 50$							
C.man	26.13	26.45	26.37	26.62	27.03	27.03	26.75
House	29.69	30.33	29.64	29.48	30.00	30.43	30.25
Peppers	26.68	26.95	26.68	27.10	27.32	27.43	27.38
Starfish	25.04	25.44	25.43	25.42	25.70	25.77	25.56
Monarch	25.82	26.32	26.26	26.31	26.78	26.88	26.54
Airplane	25.10	25.42	25.56	25.59	25.87	25.90	25.86
Parrot	25.90	26.14	26.12	26.16	26.48	26.58	26.55
Lena	29.05	29.25	29.32	28.93	29.39	29.68	29.53
Barbara	27.22	27.79	25.24	25.70	26.22	26.48	25.72
Boat	26.78	26.97	27.03	26.94	27.20	27.32	27.24
Man	26.81	26.94	27.06	26.98	27.24	27.30	27.15
Couple	26.46	26.64	26.67	26.50	26.90	27.07	27.07
Average	26.72	27.05	26.78	26.81	27.18	27.32	27.13
$\sigma = 75$							
C.man	24.32	24.6	24.63	–	25.07	25.29	25.15
House	27.51	28.24	27.78	–	27.85	28.43	28.70
Peppers	24.73	24.96	24.88	–	25.17	25.39	25.53
Starfish	23.27	23.49	23.57	–	23.64	23.82	23.55
Monarch	23.91	24.31	24.40	–	24.71	24.99	24.67
Airplane	23.48	23.74	23.87	–	24.03	24.18	24.27
Parrot	24.18	24.43	24.55	–	24.71	24.94	24.80
Lena	27.25	27.54	27.68	–	27.54	27.97	27.93
Barbara	25.12	25.81	23.39	–	23.63	24.24	23.75
Boat	25.12	25.29	25.44	–	25.47	25.64	25.55
Man	25.32	25.42	25.59	–	25.64	25.75	25.69
Couple	24.70	24.86	25.02	–	24.97	25.29	25.29
Average	24.91	25.23	25.07	–	25.2	25.49	25.41