

1 We thank the reviewers for their constructive feedback. We will incorporate these comments in the final version, and  
2 address the concerns as follows.

3 **General Comments: Regarding Experiment.** We put more experiments details in supplementary materials which  
4 includes the choice of  $\epsilon$  mentioned by reviewer#1. We also used normalized gradient and  $\epsilon$ -ball projection and we'll  
5 mention this in our next version. We would also like to thank reviewer#1 and #2 for their helpful advice about writing  
6 and typesetting, which will be properly dealt with in our next version.

### 7 Reviewer#1

8 **Regarding Stronger Attack.** We conduct experiments on stronger attack, the results show our approach can defense  
9 stronger attack. The results of PreAct-Res18 on CIFAR10 are shown as follows (average of three experiments)

	Clean	PGD-20	PGD-100	PGD-1000	CW attack
Madry	84.89±0.19	42.32±0.29	42.13±0.27	41.42±0.20	59.30±0.16
YOPO-5-3	83.51±0.22	43.94±0.20	43.17±0.17	42.52±0.36	60.18±0.38

10 **Regarding Clarity.** Thanks for pointing this out. The variable  $p$  is a "dual" variable. Thus in Theorem 1, we need to  
11 construct a  $p$  to satisfy the dual certificates. The algorithm uses an iterative scheme to find it. The variable  $p$  in the  
12 Hamiltonian is the same as the slack variable  $p$ . The definition of Hamiltonian is brought from physic and is well known  
13 in the control community. It can also be understood as a Fréchet Dual of the original problem.

14 **Regarding Free-m.** We would like to point out that the Free-m method is an independent and *concurrent* work (was  
15 put on arXiv on April 30 which was just before the NeurIPS' deadline). In our paper, we also show that their method is  
16 a special case of ours, namely YOPO- $m$ -1. The epsilon used (1-7) in Free-m paper for imagenet is wired (too small)  
17 and the accuracy is far from the state-of-the-art report [1]. Imagenet is still a hard problem mainly due to limited  
18 computation resources, and we are still working on it. ([1] Feature Denoising for Improving Adversarial Robustness  
19 arXiv:1812.03411)

20 **Regarding using the first k-layers be used for the inner-loop adversary.** It is flexible to try  $k$  other than 1, but in  
21 our experiment, selecting  $k = 1$  works the best. We will include an ablation study in the final version.

22 **Regarding the analysis of  $m$  and  $n$ .** Thanks for your suggestion and we will add more ablation study over this. The  
23 analysis could be found in Line145-154, we also use YOPO-3-5 and YOPO-5-3 to empirically justify the analysis.

### 24 Reviewer # 2

25 **Regarding Twice Continuously Differentiability.** The set of non-differentiable part of ReLU is of measure zero.  
26 Thus we do not think this will affect the algorithm a lot. The BP algorithm typically requires the activation function  
27 to be differentiable but works well empirically. Reviewers can consider there exist a really good smooth function  
28 to approximate ReLU. *First order differentiability is enough for the theory in our paper, while twice continuous*  
29 *differentiability may be required for further convergence analysis.*

30 **Regarding Theorem 2.** Theorem 2 is used to show the relationship between our algorithm and PMP, and is important  
31 for that matter.

### 32 Reviewer#3

33 **Regarding comparison with previous work.** First of all, as reviewer#1 mentioned, one of the main contributions is  
34 discovering the benefits of the control perspective in the *adversarial setting*. We agree the control perspective is not a  
35 new idea in deep learning and we have already cited the original Lecun's BP paper and other related papers. At the same  
36 time, the long training time is the *main* issue when scaling adversarial training to a larger dataset and networks. That's  
37 why most of the adversarial training papers just test CIFAR10. In our work, we showed the power of control perspective  
38 in accelerating the heavy training procedure, which we think will help the community to scale up their experiment.

39 Secondly, there seems to be some misunderstanding that our work is using control to model **feed forward network** but  
40 not **RNN**. It's **not time-homogeneous**. It is not clear to use how the BPTT algorithms could be applied in our setting.

41 Finally, our splitting method provides a new perspective on solving the optimality condition. This new perspective  
42 not only provides a description of the algorithm in a more general setting, but also inspires algorithms beyond  
43 back-propagation based training.

44 **Regarding the training time.** First of all, the computational cost (e.g. FLOP) of YOPO is theoretically smaller  
45 than the original adversarial training, typically 1/5-1/4 times smaller. The code is provided in the supplementary for  
46 reproducibility. All codes are written in Pytorch. There is also an unofficial TensorFlow code on Github showing that  
47 YOPO is quite efficient.