

1 **[[Reviewer 1]]** Thank you for your feedback. We will definitely release our code along with the camera-ready version
 2 of the manuscript. ■ **Fitting to training data:** The advantage of fitting the meta-model on sampled feature points is
 3 that the accuracy of the meta-model **would not be limited by the size of the training data**. However, if the meta-model
 4 is meant to be optimized w.r.t the feature distribution, then one can fit the feature distribution, say using a **GAN** or a
 5 **kernel density function**, and sample feature points from the estimated distribution to train the meta-model. **Fitting the**
 6 **meta-model directly on training data will correspond to a 2-layer neural network with Meijer-G function as activation**
 7 **functions (see Figure 3)**. While this is very interesting, it departs from the main objective of the paper and demands a
 8 separate analysis on generalization performance, so we will add this discussion in the supplementary material. ■ **Loss**
 9 **function & regularization:** The loss function should be selected based on the application, e.g., if f is a classifier, then
 10 ℓ should be a cross-entropy loss. The idea of adding a regularization term is also very interesting although it is not
 11 straightforward. We will investigate using the **number of poles and zeros** as a penalty term as it is a natural measure of
 12 the complexity of a G function. We will add a discussion on loss functions and regularization in the final manuscript.

13 **[[Reviewer 2]]** Thank you for your helpful comments and suggestions. ■ **Interpretability of complicated functions:**
 14 As mentioned in **lines 75 and 89**, different functional forms are deemed interpretable in different applications. Bessel
 15 functions (and other special functions) are very common in empirical physics and material sciences (e.g. wave and
 16 field equations are modeled with such functions [3, 4]). (Please also refer to response **Significance & applicability** for
 17 **Reviewer 3**.) The theoretical justification of our framework was provided in **Section 3.1**, where we have shown that
 18 — based on the **Kolomogorov superposition theorem** — our approach can approximate any multivariate continuous
 19 function. ■ **Complexity tuning:** Our algorithm explores the Pareto front of simplicity vs. predictivity systematically
 20 in two ways: (1) it uses **Bayesian optimization** to conduct hyper-parameter search by picking the smallest number
 21 of **poles and zeros for the Meijer-G function** (i.e., simplest functional form) that best fits the model, and (2) it uses
 22 **polynomial Chebyshev approximations** to simplify meta-models with complex functional forms (**Algorithm 1**). We will
 23 emphasize this in the final manuscript. ■ **Fitting to training data:** Please kindly refer to response **Fitting to training**
 24 **data for Reviewer 1**. ■ **Loss function:** Our framework does not pose limitations on the loss function being used: any
 25 differentiable loss function (e.g., cross-entropy) can be used instead of the L_2 loss in **Equation (2)**. ■ **Convexity:**
 26 In general, optimizing symbolic models with arbitrary non-linearity cannot be formulated as a convex optimization
 27 problem unless strict prior assumptions on the symbolic functions (e.g., linearity) are made (as in [8, 14]). This is why
 28 symbolic regression models resort to search algorithms based on **genetic programming**, which also does not guarantee a
 29 global solution [23-25]. Moreover, most of the competitive deep learning-based baselines such as DeepLIFT and L2X
 30 also use gradient descent. A key strength of our framework is that for the first time, flexible symbolic modeling can be
 31 conducted efficiently via gradient descent rather than exhaustive search heuristics. We believe this to be a strength of our
 32 method and not a weakness. ■ **Extra references:** We will add all the suggested references in the final the manuscript.

In addition, we have implemented two of the requested baselines and incorporated the results into **Sections 5.1 and 5.2**. The two baselines are: the **additive GP** by **Duvenaud et al.** and **ANOVA GP** by **Kaufman et al.**. As shown in
 33 the following Table, we found that neither baselines outperformed our model for **experiment 5.2**. Our interpretation for these results is that the additive GP kernel decomposition cannot capture the intricate interactions between (overlapping) feature subsets learned by the reference XGBoost model.

| | AUC-ROC |
|-------------|-----------------|
| SM | 0.8651 ± 0.0045 |
| Additive GP | 0.8502 ± 0.0062 |
| ANOVA GP | 0.8498 ± 0.0053 |

34 **[[Reviewer 3]]** Thank you for your valuable comments. ■ **Significance & applicability:** As mentioned in **lines 66-76**
 35 and **Section 4**, our method is applicable to the wide range of setups where a model’s feature importance, interactions
 36 or explicit equations are essential for understanding its instance-wise predictions or uncovering the sources of its
 37 performance gain. We demonstrated the significance of our algorithm through the exemplary medical application in
 38 **Section 5.2**, which entailed explaining the predictions of a **complex model** for breast cancer, and helped recover new
 39 feature interactions that were unknown in the clinical literature. We will make sure that these aspects regarding the
 40 significance of our work are clearly stated in the camera-ready version of the paper. ■ **Empirical evaluation:** By
 41 virtue of the Kolomogorov superposition theorem [28], our algorithm can model any multivariate continuous function
 42 regardless of its **dimensionality** and the **richness of its internal feature representations**. Our algorithm is in fact more
 43 advantageous for more complex models since gradient descent is more efficient in large parameter spaces compared to
 44 black-box optimization methods which **scale exponentially** with the number of parameters. In the final manuscript, we
 45 will add the AUC-ROC performance of symbolic regression (SR) to **Table 3**. The run-time of SR on this dataset was 3.5
 46 times longer than our algorithm. The functional form of the equation in **line 267** was the same in all 5 runs, and the
 47 variability of the coefficients across runs was statistically insignificant. We will report the variance of the coefficients
 48 in **line 267** in the supplementary material. ■ **Influence of hyper-parameters:** More complex models require more
 49 **poles and zeros** (hyper-parameters) for the corresponding meta-model. We tuned the hyper-parameters in **Section 5.2**
 50 using Bayesian optimization. ■ **Related literature:** In the final version of the paper, we will make it clear that our
 51 framework does not encompass the line of research including LRP, PatternAttribution/Net, DeepTaylor, etc, and will
 52 point out to the unifying nature of the SHAP framework. ■ **Limits on symbolic expressions:** Our approach is not
 53 limited to additive meta-models: as can be seen in equation (5), our meta-models comprise **composite (nested) functions**
 54 of additive functions of the form $\sum_j f_j(g_1^j(x_1) + \dots + g_n^j(x_n))$. By expanding these composite functions (e.g., using
 55 Taylor’s expansion) we can recover rich multiplicative terms similar to those in the expression trees of genetic models.