

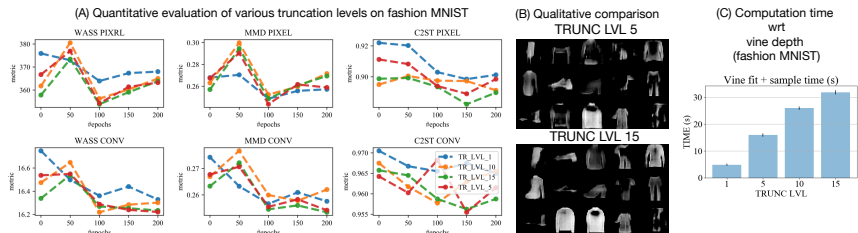
1 **Reviewer #1**

- 2 • *Introduction.* We completely agree and will further emphasize that copulas repurpose a tool learning data representa-
- 3 tions into a full-fledged generative model. Copulas allow to easily (and at a comparatively small computational cost)
- 4 turn any AE into a generative model with performances that compare favorably to state-of-the-art methods. We will
- 5 rewrite the intro and highlight this key point, it currently appears only in lines 68 - 75 and in Appendix F.
- 6 • *Gaussian copula.* We apologize for the confusion. In (2), $\mathcal{N}_{(\Phi^{-1}(u_j), \Phi^{-1}(v_j)), \Sigma)}$ is a bivariate Gaussian distribution
- 7 with mean $(\Phi^{-1}(u_j), \Phi^{-1}(v_j))$ where $\{u_j, v_j\}_{j=1}^n$ are the observations. (2) defines a kernel estimator of the copula
- 8 density and not a Gaussian copula. We only present Gaussian copulas in Figures 3 and 4 to show how the Gaussianity
- 9 assumption results in worse synthetic samples compared to the nonparametric copulas. We will clarify this in the text.
- 10 • *Typos, restructuring, and clarifying captions.* Thank you for the comments, we agree and will correct as suggested.
- 11 • *Conclusion.* An executive summary of the empirical results is indeed lacking in the conclusion and will be added.

12 **Reviewer #2**

- 13 • *Contributions.* We agree that the paper is fairly practical rather than theoretical, but simple and simplistic should not
- 14 be confused. Given the general interest in generative modeling, we feel like a method allowing to repurpose AEs into
- 15 generative models at a small computational cost is worthy in itself.
- 16 • *Presentation of concepts/models/algorithms.* We will extend each topic in the supplementary to make the paper as
- 17 self-contained as possible. But note that the pseudo-observations are already described lines 96-97 and in Figure 2,
- 18 no model selection of copulas is required since only nonparametric pairs are used, sequential estimation is described
- 19 over 11 lines while referencing to the rich literature on the topic, and nonparametric estimation takes about half a
- 20 page. Basic concepts such as Sklar’s theorem/copula definition take only 3 lines + 4 for the density (will cut 1/2), and
- 21 AEs take 11 lines before switching to generative modeling (hard to cut). Vine copulas have generated thousands of
- 22 papers in the last decade and, given the space constraint, we restricted ourselves to two pages (1/4 of the paper).
- 23 • *Copula selection.* As mentioned, no selection is required since (2) (i.e., nonparametric copulas) is used for every pair.
- 24 • *Complexity.* We will add to the paper that complexity $\approx O(n \times \dim \times \text{trunc_lvl})$ for estimation/sampling algorithms,
- 25 both involving a double loop over dimension/trunc level with an internal step scaling linearly with the sample size.
- 26 • *Quality of the samples and truncation.* We will add an extended analysis. See the figure below for preliminary results
- 27 suggesting that deeper vines (i.e., longer computation times) improves the quality of the generated samples. Note
- 28 also the linear scaling of computation time with truncation level.
- 29 • *Continuity/differentiability.* We will add the needed assumptions for the asymptotic properties of (2) as in [19].
- 30 • *Advantages over VAEs and GANs.* Due to space constraints, the analysis detailed the comments of lines 68-75 was
- 31 moved to Appendix F. We will add it back (see a similar comment from Rev#1). Regarding complexity, our claim is
- 32 simply that VCAEs are easier to train. We will also describe better the results from the different metrics.

33 • *Typos and mistakes.* Thank you for spotting them, we agree, will correct all, and proofread better. Page 3, Appendix A.2 should be Figure 2. D_e is indeed a subset, but the other two are “elements of”. Figures 2/3, yes and yes.



34 **Reviewer #3**

- 35 • *Conclusiveness of results.* This paper is a first-attempt at an alternative approach to seamlessly construct generative
- 36 models by combining vines and AEs, and we chose arguably the three most common datasets and two best known
- 37 competitors to illustrate our method’s potential. The aim was neither an extensive empirical analysis, nor it was to
- 38 prove definitive superiority against all state-of-the-art methods. In any case, Fashion MNIST will be added following
- 39 the preliminary analysis from the figure above.
- 40 • *Formula 2.* Agreed, it also have been confusing to Rev#1, we could write something like $\mathcal{N}_{\mu, \Sigma}$ where $\mu = \dots$
- 41 • *Fig 3 contours.* We should have written the contours are presented in the kernel space, i.e. after transformation to
- 42 Gaussian margins (lines 172-174) and circular because X_1 and X_2 are independent.
- 43 • *Intuition for sharper images.* Two potential explanations will be added. First, blurriness in VAEs comes from the
- 44 independence and Gaussianity assumptions for the latent features, but we do not assume this. Second, adding depth
- 45 (trees) to the vine structure results in more dependencies/details captured, and hence sharper images.
- 46 • *Fig 4.* Sorry for the mix-up, the middle and right panels correspond respectively to samples for MNIST and SVNH.
- 47 • *Fig 6 for MNIST and CelebA.* The experiments were not finished by the deadline but will be added to the final version.
- 48 Preliminary results indicate that the conclusions will be similar as for SVNH.
- 49 • *Fig 7 and proofreading.* Thanks for noticing about Fig 7, and proofreading was also asked by Rev#2, our apologies.
- 50 • *Memorizing in Fig 7.* Since a vine is estimated on the latent features, memorization is rather the AE’s issue. Because
- 51 of the struggle in the community over how to tackle memorization evaluation (see e.g. Theis et al. , 2016, Borji 2018),
- 52 we thought it to be out of the score of this work, but we will mention it.