
Supplementary Material

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1 Hyperparameter Settings

2 Throughout all experiments, we use Adam [8] for optimizing the baseline function and the autoen-
3 coder. Hyperparameters for rllab experiments are summarized in Table 1. Here the policy takes
4 a state s as input, and outputs a Gaussian distribution $\mathcal{N}(\mu(s), \sigma^2)$, where $\mu(s)$ is the output of a
5 multi-layer perceptron (MLP) with tanh nonlinearity, and $\sigma > 0$ is a state-independent parameter.

Table 1: TRPO hyperparameters for rllab experiments

Experiment	MountainCar	CartPoleSwingUp	HalfCheetah	SwimmerGatherer
TRPO batch size	5k	5k	5k	50k
TRPO step size			0.01	
Discount factor γ			0.99	
Policy hidden units	(32, 32)	(32,)	(32, 32)	(64, 32)
Baseline function	linear	linear	linear	MLP: 32 units
Exploration bonus			$\beta = 0.01$	
SimHash dimension			$k = 32$	

6 Hyperparameters for Atari 2600 experiments are summarized in Table 2 and 3. By default, all
7 convolutional layers are followed by ReLU nonlinearity.

Table 2: TRPO hyperparameters for Atari experiments with image input

Experiment	TRPO-pixel-SimHash	TRPO-BASS-SimHash	TRPO-AE-SimHash
TRPO batch size		100k	
TRPO step size		0.01	
Discount factor		0.995	
# random seeds	5	5	3
Input preprocessing	grayscale; downsampled to 52×52 ; each pixel rescaled to $[-1, 1]$ 4 previous frames are concatenated to form the input state		
Policy structure	16 conv filters of size 8×8 , stride 4 32 conv filters of size 4×4 , stride 2 fully-connect layer with 256 units linear transform and softmax to output action probabilities (use batch normalization[7] at every layer)		
Baseline structure	(same as policy, except that the last layer is a single scalar)		
Exploration bonus		$\beta = 0.01$	
Hashing parameters	$k = 256$	cell size $C = 20$ $B = 20$ bins	$b(s)$ size: 256 bits downsampled to 64 bits

8 The autoencoder architecture was shown in Figure 1 of Section 2.3. Specifically, uniform noise
9 $U(-a, a)$ with $a = 0.3$ is added to the sigmoid activations. The loss function Eq.(3) (in the main

Table 3: TRPO hyperparameters for Atari experiments with RAM input

Experiment	TRPO-RAM-SimHash
TRPO batch size	100k
TRPO step size	0.01
Discount factor	0.995
# random seeds	10
Input preprocessing	vector of length 128 in the range $[0, 255]$; downsampled to $[-1, 1]$
Policy structure	MLP: (32, 32, number_of_actions), tanh
Baseline structure	MLP: (32, 32, 1), tanh
Exploration bonus	$\beta = 0.01$
SimHash dimension	$k = 256$

10 text), using $\lambda = 10$, is updated every $j_{\text{update}} = 3$ iterations. The architecture looks as follows: an
 11 input layer of size 52×52 , representing the image luminance is followed by 3 consecutive 6×6
 12 convolutional layers with stride 2 and 96 filters feed into a fully connected layer of size 1024, which
 13 connects to the binary code layer. This binary code layer feeds into a fully-connected layer of 1024
 14 units, connecting to a fully-connected layer of 2400 units. This layer feeds into 3 consecutive 6×6
 15 transposed convolutional layers of which the final one connects to a pixel-wise softmax layer with 64
 16 bins, representing the pixel intensities. Moreover, label smoothing is applied to the different softmax
 17 bins, in which the log-probability of each of the bins is increased by 0.003, before normalizing. The
 18 softmax weights are shared among each pixel.

19 In addition, we apply counting Bloom filters [5] to maintain a small hash table. Details can be found
 20 in Appendix 4.

21 **2 Description of the Adapted rllab Tasks**

22 This section describes the continuous control environments used in the experiments. The tasks are
 23 implemented as described in [4], following the sparse reward adaptation of [6]. The tasks have the
 24 following state and action dimensions: CartPoleSwingup, $\mathcal{S} \subseteq \mathbb{R}^4$, $\mathcal{A} \subseteq \mathbb{R}$; MountainCar $\mathcal{S} \subseteq \mathbb{R}^3$,
 25 $\mathcal{A} \subseteq \mathbb{R}^1$; HalfCheetah, $\mathcal{S} \subseteq \mathbb{R}^{20}$, $\mathcal{A} \subseteq \mathbb{R}^6$; SwimmerGather, $\mathcal{S} \subseteq \mathbb{R}^{33}$, $\mathcal{A} \subseteq \mathbb{R}^2$. For the sparse
 26 reward experiments, the tasks have been modified as follows. In CartPoleSwingup, the agent receives
 27 a reward of +1 when $\cos(\beta) > 0.8$, with β the pole angle. In MountainCar, the agent receives
 28 a reward of +1 when the goal state is reached, namely escaping the valley from the right side.
 29 Therefore, the agent has to figure out how to swing up the pole in the absence of any initial external
 30 rewards. In HalfCheetah, the agent receives a reward of +1 when $x_{\text{body}} > 5$. As such, it has to figure
 31 out how to move forward without any initial external reward. The time horizon is set to $T = 500$ for
 32 all tasks.

33 **3 Analysis of Learned Binary Representation**

34 Figure 1 shows the downsampled codes learned by the autoencoder for several Atari 2600 games
 35 (Frostbite, Freeway, and Montezuma’s Revenge). Each row depicts 50 consecutive frames (from 0 to
 36 49, going from left to right, top to bottom). The pictures in the right column depict the binary codes
 37 that correspond with each of these frames (one frame per row). Figure 2 shows the reconstructions
 38 of several subsequent images according to the autoencoder. Some binaries stay consistent across
 39 frames, and some appear to respond to specific objects or events. Although the precise meaning of
 40 each binary number is not immediately obvious, the figure suggests that the learned hash code is a
 41 reasonable abstraction of the game state.

42 **4 Counting Bloom Filter/Count-Min Sketch**

43 We experimented with directly building a hashing dictionary with keys $\phi(s)$ and values the state
 44 counts, but observed an unnecessary increase in computation time. Our implementation converts the
 45 integer hash codes into binary numbers and then into the “bytes” type in Python. The hash table is a
 46 dictionary using those bytes as keys.

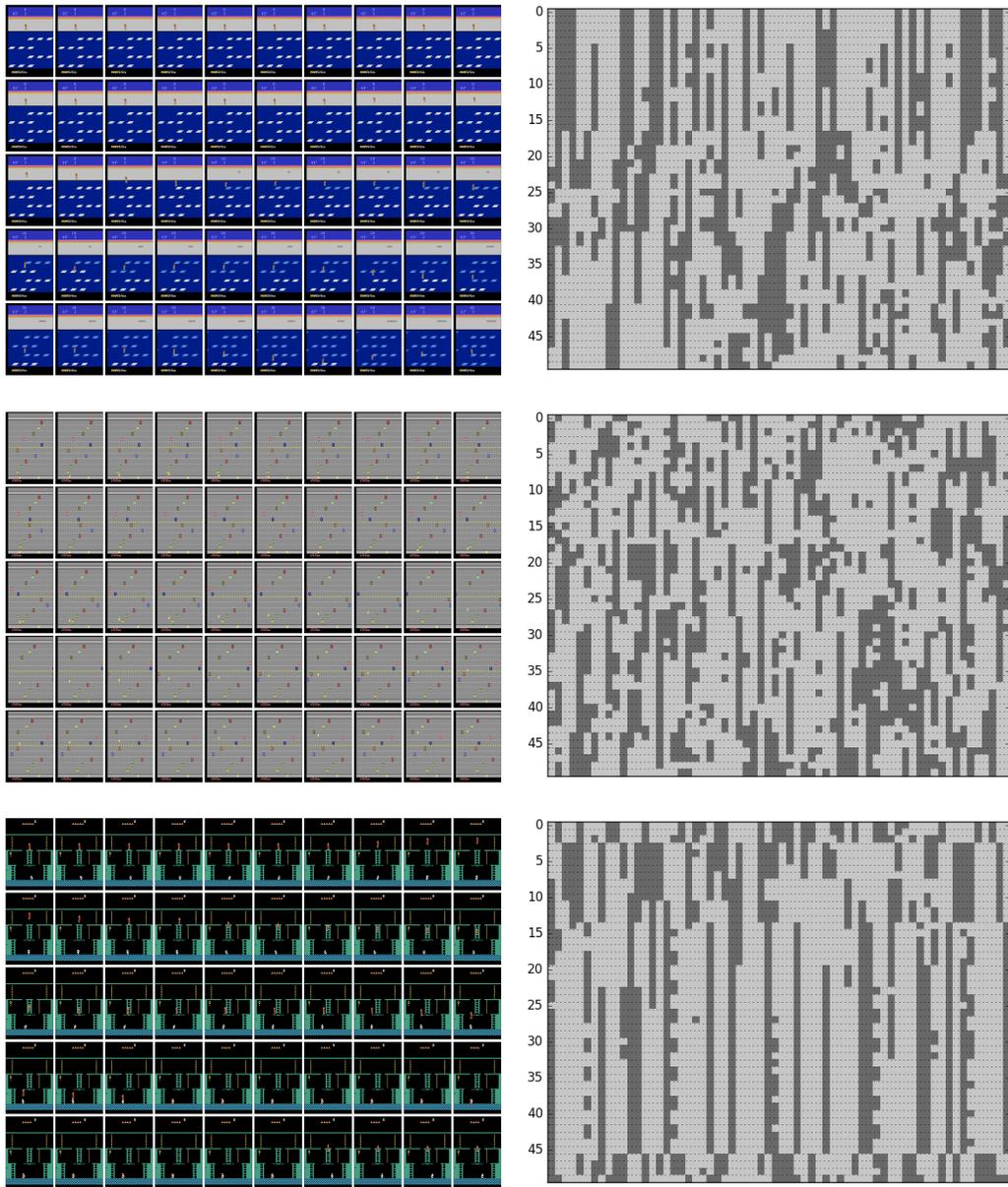


Figure 1: Frostbite, Freeway, and Montezuma's Revenge: subsequent frames (left) and corresponding code (right); the frames are ordered from left (starting with frame number 0) to right, top to bottom; the vertical axis in the right images correspond to the frame number.

47 However, an alternative technique called Count-Min Sketch [3], with a data structure identical
 48 to counting Bloom filters [5], can count with a fixed integer array and thus reduce computation
 49 time. Specifically, let p^1, \dots, p^l be distinct large prime numbers and define $\phi^j(s) = \phi(s) \bmod p^j$.
 50 The count of state s is returned as $\min_{1 \leq j \leq l} n^j(\phi^j(s))$. To increase the count of s , we increment
 51 $n^j(\phi^j(s))$ by 1 for all j . Intuitively, the method replaces ϕ by weaker hash functions, while it reduces
 52 the probability of over-counting by reporting counts agreed by all such weaker hash functions. The
 53 final hash code is represented as $(\phi^1(s), \dots, \phi^l(s))$.

54 Throughout all experiments above, the prime numbers for the counting Bloom filter are 999931,
 55 999953, 999959, 999961, 999979, and 999983, which we abbreviate as “6 M”. In addition, we
 56 experimented with 6 other prime numbers, each approximately 15 M, which we abbreviate as “90 M”.
 57 As we can see in Figure 3, counting states with a dictionary or with Bloom filters lead to similar
 58 performance, but the computation time of latter is lower. Moreover, there is little difference between
 59 direct counting and using a very larger table for Bloom filters, as the average bonus rewards are
 60 almost the same, indicating the same degree of exploration-exploitation trade-off. On the other hand,
 61 Bloom filters require a fixed table size, which may not be known beforehand.

62 **Theory of Bloom Filters** Bloom filters [2] are popular for determining whether a data sample s'
 63 belongs to a dataset \mathcal{D} . Suppose we have l functions ϕ^j that independently assign each data sample
 64 to an integer between 1 and p uniformly at random. Initially $1, 2, \dots, p$ are marked as 0. Then every
 65 $s \in \mathcal{D}$ is “inserted” through marking $\phi^j(s)$ as 1 for all j . A new sample s' is reported as a member
 66 of \mathcal{D} only if $\phi^j(s)$ are marked as 1 for all j . A bloom filter has zero false negative rate (any $s \in \mathcal{D}$ is
 67 reported a member), while the false positive rate (probability of reporting a nonmember as a member)
 68 decays exponentially in l .

69 Though Bloom filters support data insertion, it does not allow data deletion. Counting Bloom filters
 70 [5] maintain a counter $n(\cdot)$ for each number between 1 and p . Inserting/deleting s corresponds
 71 to incrementing/decrementing $n(\phi^j(s))$ by 1 for all j . Similarly, s is considered a member if
 72 $\forall j : n(\phi^j(s)) = 0$.

73 Count-Min sketch is designed to support memory-efficient counting without introducing too many
 74 over-counts. It maintains a separate count n^j for each hash function ϕ^j defined as $\phi^j(s) = \phi(s)$
 75 $\bmod p^j$, where p^j is a large prime number. For simplicity, we may assume that $p^j \approx p \forall j$ and ϕ^j
 76 assigns s to any of $1, \dots, p$ with uniform probability.

77 We now derive the probability of over-counting. Let s be a fixed data sample (not necessarily
 78 inserted yet) and suppose a dataset \mathcal{D} of N samples are inserted. We assume that $p^l \gg N$. Let
 79 $n := \min_{1 \leq j \leq l} n^j(\phi^j(s))$ be the count returned by the Bloom filter. We are interested in computing
 80 $\text{Prob}(n > 0 | s \notin \mathcal{D})$. Due to assumptions about ϕ^j , we know $n^j(\phi^j(s)) \sim \text{Binomial}\left(N, \frac{1}{p}\right)$.
 81 Therefore,

$$\begin{aligned}
 \text{Prob}(n > 0 | s \notin \mathcal{D}) &= \frac{\text{Prob}(n > 0, s \notin \mathcal{D})}{\text{Prob}(s \notin \mathcal{D})} \\
 &= \frac{\text{Prob}(n > 0) - \text{Prob}(s \in \mathcal{D})}{\text{Prob}(s \notin \mathcal{D})} \\
 &\approx \frac{\text{Prob}(n > 0)}{\text{Prob}(s \notin \mathcal{D})} \\
 &= \frac{\prod_{j=1}^l \text{Prob}(n^j(\phi^j(s)) > 0)}{(1 - 1/p^l)^N} \\
 &= \frac{(1 - (1 - 1/p)^N)^l}{(1 - 1/p^l)^N} \\
 &\approx \frac{(1 - e^{-N/p})^l}{e^{-N/p^l}} \\
 &\approx (1 - e^{-N/p})^l.
 \end{aligned} \tag{1}$$

82 In particular, the probability of over-counting decays exponentially in l . We refer the readers to [3]
 83 for other properties of the Count-Min sketch.

84 5 Robustness Analysis

85 5.1 Granularity

86 While our proposed method is able to achieve remarkable results without requiring much tuning,
87 the granularity of the hash function should be chosen wisely. Granularity plays a critical role in
88 count-based exploration, where the hash function should cluster states without under-generalizing
89 or over-generalizing. Table 4 summarizes granularity parameters for our hash functions. In Table 5
90 we summarize the performance of TRPO-pixel-SimHash under different granularities. We choose
91 Frostbite and Venture on which TRPO-pixel-SimHash outperforms the baseline, and choose as reward
92 bonus coefficient $\beta = 0.01 \times \frac{256}{k}$ to keep average bonus rewards at approximately the same scale.
93 $k = 16$ only corresponds to 65536 distinct hash codes, which is insufficient to distinguish between
94 semantically distinct states and hence leads to worse performance. We observed that $k = 512$ tends
95 to capture trivial image details in Frostbite, leading the agent to believe that every state is new and
96 equally worth exploring. Similar results are observed while tuning the granularity parameters for
97 TRPO-BASS-SimHash and TRPO-AE-SimHash.

Table 4: Granularity parameters of various hash functions

SimHash	k : size of the binary code
BASS	C : cell size
	B : number of bins for each color channel
AE	k : downstream SimHash parameter
	λ : binarization parameter
SmartHash	s : grid size agent (x, y) coordinates

Table 5: Average score at 50 M time steps achieved by TRPO-pixel-SimHash

k	16	64	128	256	512
Frostbite	3326	4029	3932	4683	1117
Venture	0	218	142	263	306

98 The best granularity depends on both the hash function and the MDP. While adjusting granularity
99 parameter, we observed that it is important to lower the bonus coefficient as granularity is increased.
100 This is because a higher granularity is likely to cause lower state counts, leading to higher bonus
101 rewards that may overwhelm the true rewards.

102 Apart from the experimental results shown in Table 1 in the main text and Table 5, additional
103 experiments have been performed to study several properties of our algorithm.

104 5.2 Hyperparameter sensitivity

105 To study the performance sensitivity to hyperparameter changes, we focus on evaluating TRPO-
106 RAM-SimHash on the Atari 2600 game Frostbite, where the method has a clear advantage over the
107 baseline. Because the final scores can vary between different random seeds, we evaluated each set of
108 hyperparameters with 30 seeds. To reduce computation time and cost, RAM states are used instead
109 of image observations.

110 The results are summarized in Table 6. Herein, k refers to the length of the binary code for hashing
111 while β is the multiplicative coefficient for the reward bonus, as defined in Section 2.2 of the main
112 text. This table demonstrates that most hyperparameter settings outperform the baseline ($\beta = 0$)
113 significantly. Moreover, the final scores show a clear pattern in response to changing hyperparameters.
114 Small β -values lead to insufficient exploration, while large β -values cause the bonus rewards to
115 overwhelm the true rewards. With a fixed k , the scores are roughly concave in β , peaking at around
116 0.2. Higher granularity k leads to better performance. Therefore, it can be concluded that the
117 proposed exploration method is robust to hyperparameter changes in comparison to the baseline, and
118 that the best parameter settings can be obtained from a relatively coarse-grained grid search.

Table 6: TRPO-RAM-SimHash performance robustness to hyperparameter changes on Frostbite

k	β							
	0	0.01	0.05	0.1	0.2	0.4	0.8	1.6
–	397	–	–	–	–	–	–	–
64	–	879	2464	2243	2489	1587	1107	441
128	–	1475	4248	2801	3239	3621	1543	395
256	–	2583	4497	4437	7849	3516	2260	374

Table 7: Average score at 50 M time steps achieved by TRPO-SmartHash on Montezuma’s Revenge (RAM observations)

s	1	5	10	20	40	60
score	2598	2500	3533	3025	2500	1921

Table 8: Interpretation of particular RAM entries in Montezuma’s Revenge

ID	Group	Meaning
3	room	room number
42	agent	x coordinate
43	agent	y coordinate
52	agent	orientation (left/right)
27	beams	on/off
83	beams	beam countdown (on: 0, off: 36 \rightarrow 0)
0	counter	counts from 0 to 255 and repeats
55	counter	death scene countdown
67	objects	Doors, skull, and key in 1st room
47	skull	x coordinate (1st and 2nd room)

119 **5.3 A Case Study of Montezuma’s Revenge**

120 Montezuma’s Revenge is widely known for its extremely sparse rewards and difficult exploration
 121 [1]. While our method does not outperform [1] on this game, we investigate the reasons behind this
 122 through various experiments. The experiment process below again demonstrates the importance of a
 123 hash function having the correct granularity and encoding relevant information for solving the MDP.

124 Our first attempt is to use game RAM states instead of image observations as inputs to the policy,
 125 which leads to a game score of 2500 with TRPO-BASS-SimHash. Our second attempt is to manually
 126 design a hash function that incorporates domain knowledge, called *SmartHash*, which uses an
 127 integer-valued vector consisting of the agent’s (x, y) location, room number and other useful RAM
 128 information as the hash code. The best SmartHash agent is able to obtain a score of 3500. Still
 129 the performance is not optimal. We observe that a slight change in the agent’s coordinates does
 130 not always result in a semantically distinct state, and thus the hash code may remain unchanged.
 131 Therefore we choose grid size s and replace the x coordinate by $\lfloor (x - x_{\min})/s \rfloor$ (similarly for y).
 132 The bonus coefficient is chosen as $\beta = 0.01\sqrt{s}$ to maintain the scale relative to the true reward¹ (see
 133 Table 7). Finally, the best agent is able to obtain 6600 total rewards after training for 1000 iterations
 134 (1000 M time steps), with a grid size $s = 10$.

¹The bonus scaling is chosen by assuming all states are visited uniformly and the average bonus reward should remain the same for any grid size.

Table 9: Performance comparison between state counting (left of the slash) and state-action counting (right of the slash) using TRPO-RAM-SimHash on Frostbite

k	β						
	0.01	0.05	0.1	0.2	0.4	0.8	1.6
64	879 / 976	2464 / 1491	2243 / 3954	2489 / 5523	1587 / 5985	1107 / 2052	441 / 742
128	1475 / 808	4248 / 4302	2801 / 4802	3239 / 7291	3621 / 4243	1543 / 1941	395 / 362
256	2583 / 1584	4497 / 5402	4437 / 5431	7849 / 4872	3516 / 3175	2260 / 1238	374 / 96

135 Table 8 lists the semantic interpretation of certain RAM entries in Montezuma’s Revenge. SmartHash,
 136 as described in Section 5.3, makes use of RAM indices 3, 42, 43, 27, and 67. “Beam walls” are
 137 deadly barriers that occur periodically in some rooms.

138 During our pursuit, we had another interesting discovery that the ideal hash function should not
 139 simply cluster states by their visual similarity, but instead by their relevance to solving the MDP. We
 140 experimented with including enemy locations in the first two rooms into SmartHash ($s = 10$), and
 141 observed that average score dropped to 1672 (at iteration 1000). Though it is important for the agent
 142 to dodge enemies, the agent also erroneously “enjoys” watching enemy motions at distance (since
 143 new states are constantly observed) and “forgets” that his main objective is to enter other rooms. An
 144 alternative hash function keeps the same entry “enemy locations”, but instead only puts randomly
 145 sampled values in it, which surprisingly achieves better performance (3112). However, by ignoring
 146 enemy locations altogether, the agent achieves a much higher score (5661) (see Figure 4). In retrospect,
 147 we examine the hash codes generated by BASS-SimHash and find that codes clearly distinguish
 148 between visually different states (including various enemy locations), but fails to emphasize that the
 149 agent needs to explore different rooms. Again this example showcases the importance of encoding
 150 relevant information in designing hash functions.

151 5.4 State and state-action counting

152 Continuing the results in Table 6, the performance of state-action counting is studied using the same
 153 experimental setup, summarized in Table 9. In particular, a bonus reward $r^+(s, a) = \frac{\beta}{\sqrt{n(s, a)}}$ instead
 154 of $r^+(s) = \frac{\beta}{\sqrt{n(s)}}$ is assigned. These results show that the relative performance of state counting
 155 compared to state-action counting depends highly on the selected hyperparameter settings. However,
 156 we notice that the best performance is achieved using state counting with $k = 256$ and $\beta = 0.2$.

157 References

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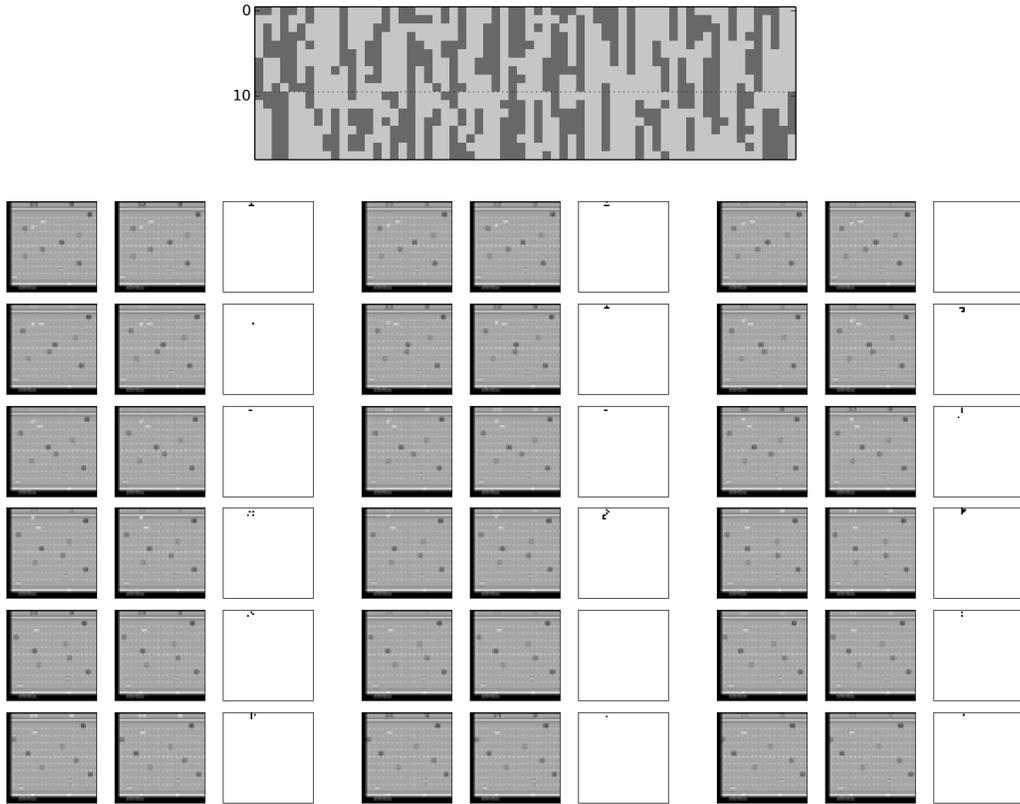


Figure 2: Freeway: subsequent frames and corresponding code (top); the frames are ordered from left (starting with frame number 0) to right, top to bottom; the vertical axis in the right images correspond to the frame number. Within each image, the left picture is the input frame, the middle picture the reconstruction, and the right picture, the reconstruction error.

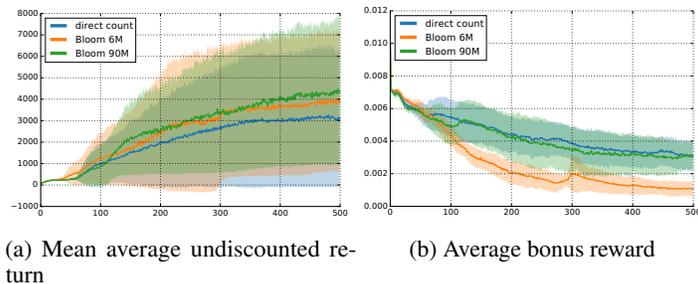


Figure 3: Statistics of TRPO-pixel-SimHash ($k = 256$) on Frostbite. Solid lines are the mean, while the shaded areas represent the one standard deviation. Results are derived from 10 random seeds. Direct counting with a dictionary uses 2.7 times more computations than counting Bloom filters (6 M or 90 M).

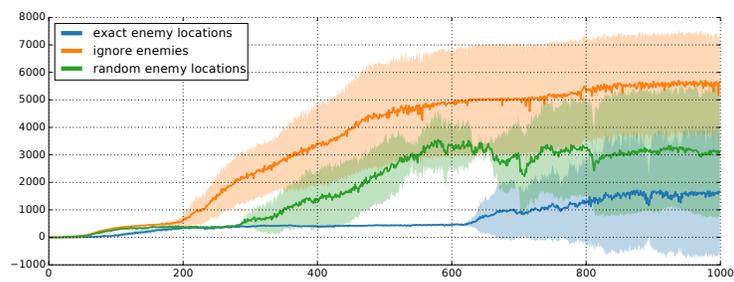


Figure 4: SmartHash results on Montezuma's Revenge (RAM observations): the solid line is the mean average undiscounted return per iteration, while the shaded areas represent the one standard deviation, over 5 seeds.